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# **Implementation and Testing of EQUISOLV II in the CMAQ Modeling System**

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# Acknowledgments

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- **NOAA:** Project Sponsor
- **Ken Schere, Prakash Bhave, and Shaocai Yu,** U.S. NOAA/EPA, for providing all input files for setting up the SOS episode and Fortran script for statistical calculations.
- **Alice Gilliland and Steve Howard,** U.S. NOAA/EPA, for providing Fortran code for extracting data from observational databases and CMAQ.
- **Eric Edgerton and Rick Saylor,** ARA, Inc., for providing the SEARCH database.
- **Ping Liu, Kai Wang, and Jianlin Hu,** NCSU, for help in post-processing model results.

# Presentation Outline

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- **Background and Objectives**
- **Box Model Comparison**
- **3-D Testing and Evaluation**
  - Episode, Model Configuration, Available Measurements
  - Preliminary Results
- **Summary and Future Work**

# Background and Objectives

- **Background**
  - Thermodynamic equilibrium affects gas-particle partitioning and PM formation (e.g., nitrate, ammonium, chloride);
  - Uncertainties in experimental data (e.g., activity coefficients, DRH);
  - Numerical difficulties in simulating a mixed-phase system;
  - Existing modules are computationally efficient but numerically less accurate and vice versa.
- **Objectives**
  - Improve EQUISOLV II in terms of numerical accuracy and computational speed;
  - Incorporate EQUISOLV II into CMAQ and CMAQ-MADRID as an alternative thermodynamic module to ISORRPIA;
  - Apply and evaluate CMAQ-EQUISOLV II's performance for the 12-28 June 1999 episode.

# Main Features of ISORROPIA and EQUISOLV II

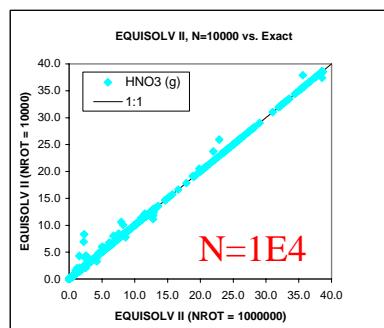
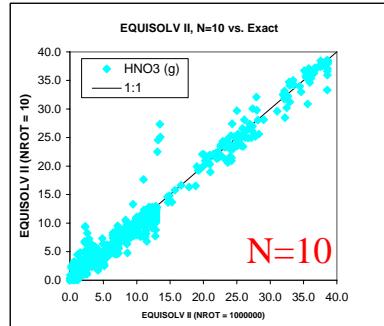
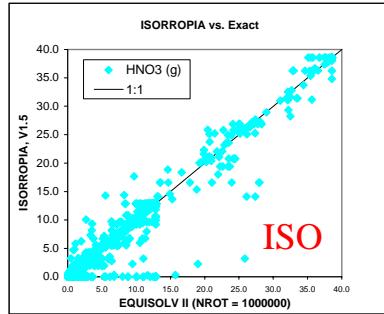
	ISORROPIA	EQUISOLV II
System solved	$\text{NH}_4\text{-Na-NO}_3\text{-SO}_4\text{-Cl}$	$\text{NH}_4\text{-Na-Ca-Mg-K-NO}_3\text{-SO}_4\text{-Cl-CO}_3$
Equilibrium reaction/ chemical species	15 reactions 21 species ( 3 gases, 9 liquids, 9 solids)	18 reactions 26 species ( 4 gases, 13 liquids, 9 solids)
Solution method	Iterative bisection Iterative bisection-Newton for $\text{H}^+$	Mass Flux Iteration (MFI) and Analytical Equilibrium Iteration (AEI)
Chemical regime	Subdomains (sulfate very rich/rich/poor)	Full domain
Activity coefficient	Binary - Kusik and Meissner, 1978 Multi-component – Bromley, 1973 Precalculated lookup table	Binary - Hamer and Wu, 1972; Goldberg, 1981; Bassett and Seinfeld, 1984; Filippov et al., 1985; and Pitzer, 1991 Multi-component - Bromley method, 1973 Precalculated lookup tables
Temperature-dependence	Equilibrium constants, DRHs	Equilibrium constants, DRHs, activity coefficients, solute and water activity coefficients down to 190 K for several species
Solid treatment	(1) Solid formed when $\text{RH} < \text{MDRH}$ (meta-stable) (2) No solid formation for all RHs (liquid only)	(1) Solid formed when $\text{RH} < \text{CRH}$ (meta-stable) (2) Solid formed when $\text{RH} < \text{DRH}$ (stable) (3) No solid formation for all RHs (liquid only)
Size-resolved equilibrium	No	Yes
3-D implementation	Single-cell only	(1) Single-cell (2) Multiple-cell (vectorization)
Reference	Nenes et al., 1998, 1999	Jacobson et al., 1996; Jacobson, 1999 a & b

# Box Model Test Conditions

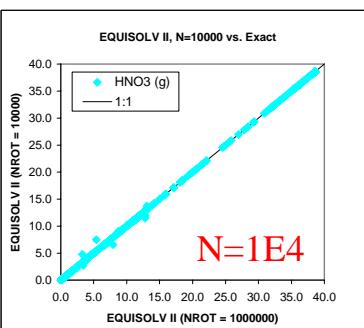
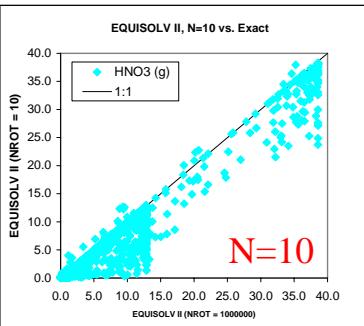
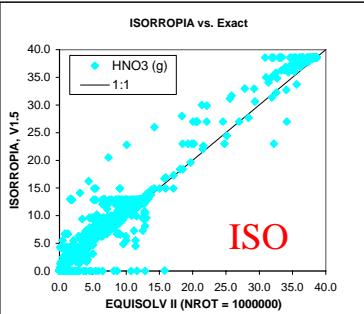
[H <sub>2</sub> SO <sub>4</sub> ], µg m <sup>-3</sup>	5	20
TNH <sub>4</sub> /TSO <sub>4</sub>	2 -16	0.5 - 4
TNO <sub>3</sub> /TSO <sub>4</sub>	1.32 - 12	0.33 -3
TNaCl/TSO <sub>4</sub>	0, 2-8	0, 0.5-2
Temperature, K	278, 288, 298, 308	278, 288, 298, 308
RH, %	1-100	1-100
Solid treatment	Solid formed when RH < CRH; No solid for all RHs	Solid formed when RH < CRH; No solid for all RHs
Iteration number used in EQUISOLV II, N	10, 100, 10000, 1000000 <b>Benchmark: 1000000</b>	10, 100, 10000, 1000000 <b>Benchmark: 1000000</b>
Total number of cases	1120	1120
Total number of simulations	(1120 + 1120 × 4 N) × 2 solid treatments = 11,200	(1120 + 1120 × 4 N) × 2 solid treatments = 11,200

# Box Model Results: HNO<sub>3</sub>(g)

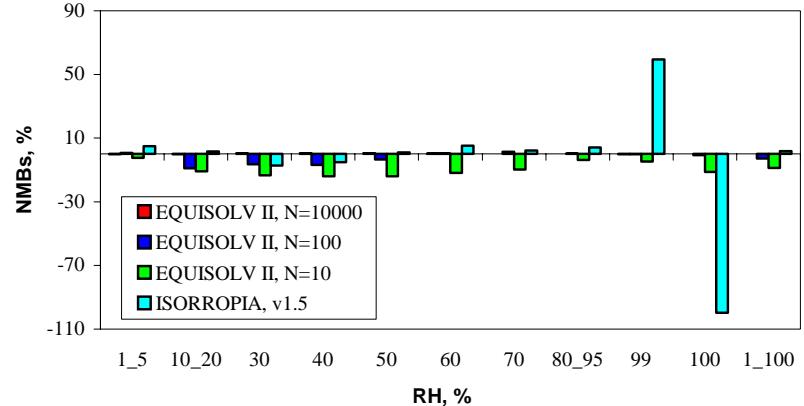
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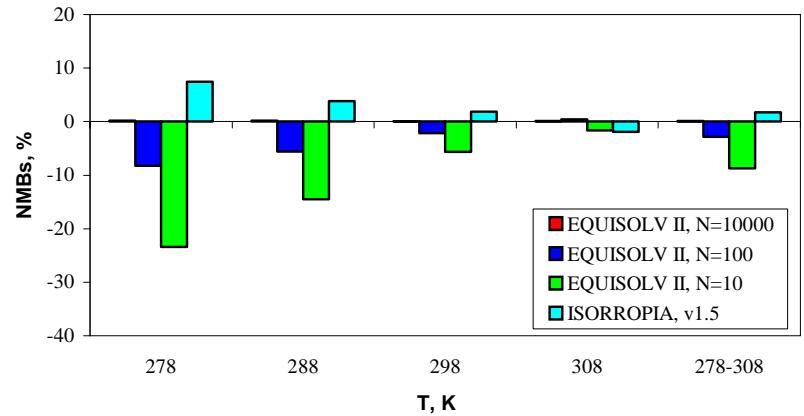
**TSO4 = 20**



NMBs for HNO<sub>3</sub>(g) at T = 278-308 K, RH = 1-100%, and [TSO4]=5, 20 ug m<sup>-3</sup>

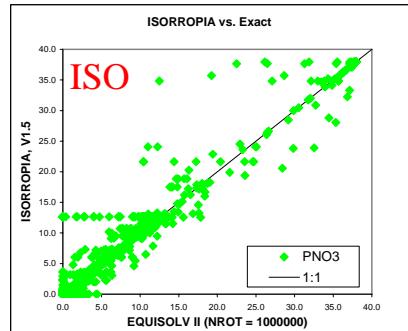


NMBs for HNO<sub>3</sub>(g) at T = 278-308 K, RH = 1-100%, and [TSO4]=5, 20 ug m<sup>-3</sup>

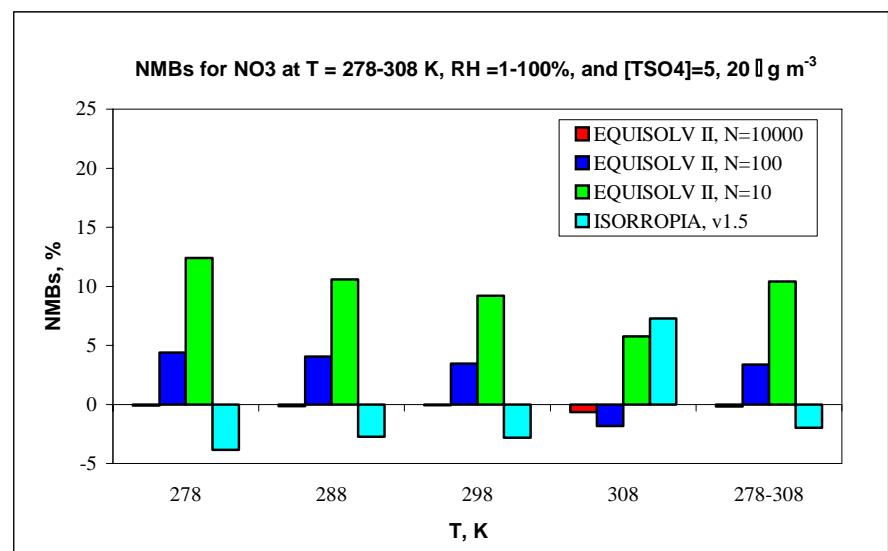
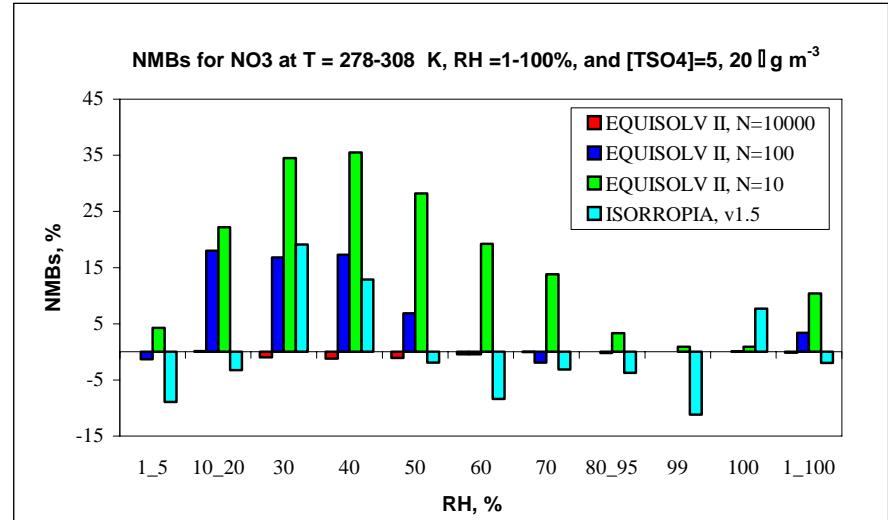
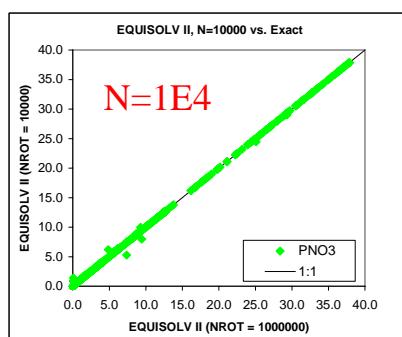
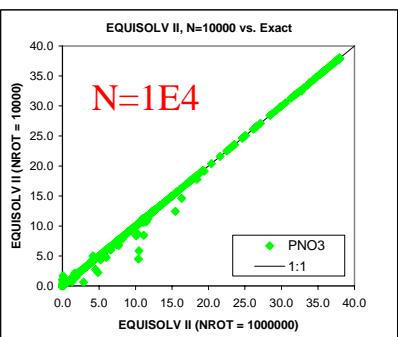
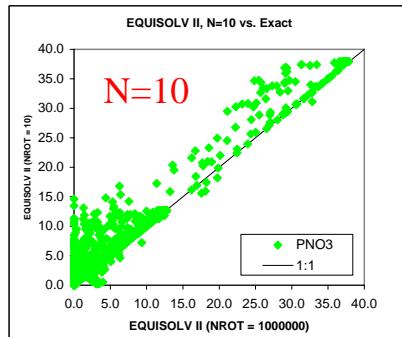
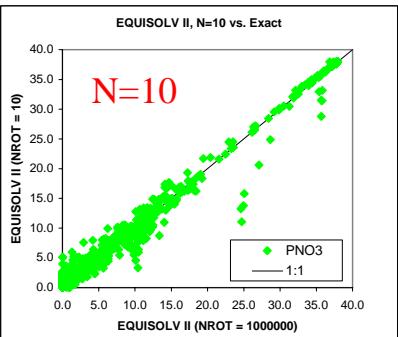
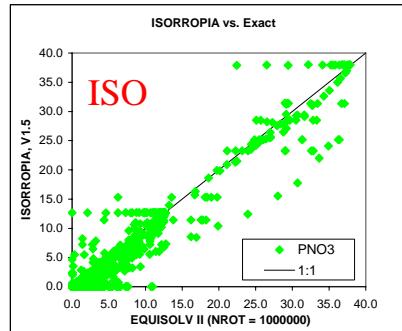


# Box Model Results: $\text{NO}_3^-$

$\text{TSO4} = 5$

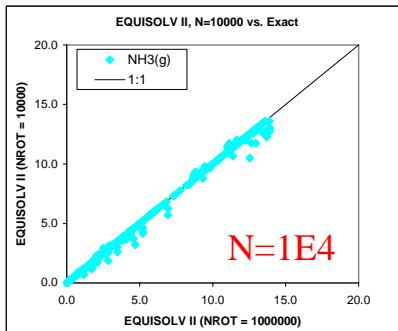
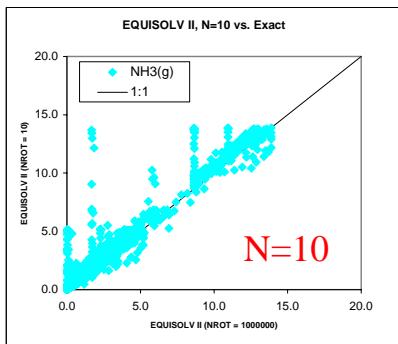
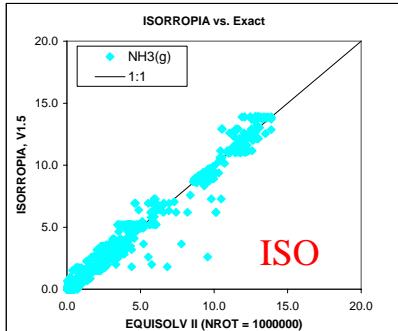


$\text{TSO4} = 20$

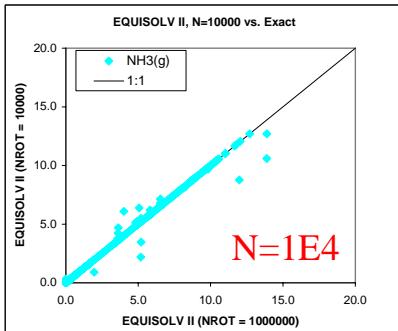
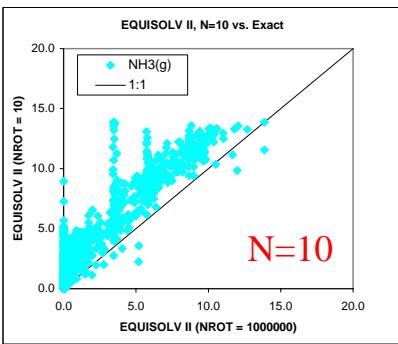
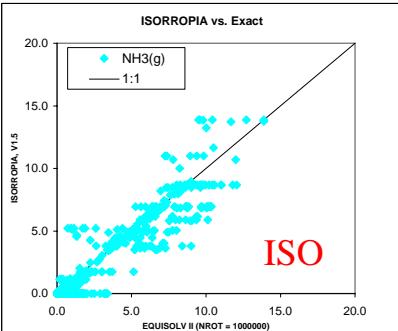


# Box Model Results: NH<sub>3</sub>(g)

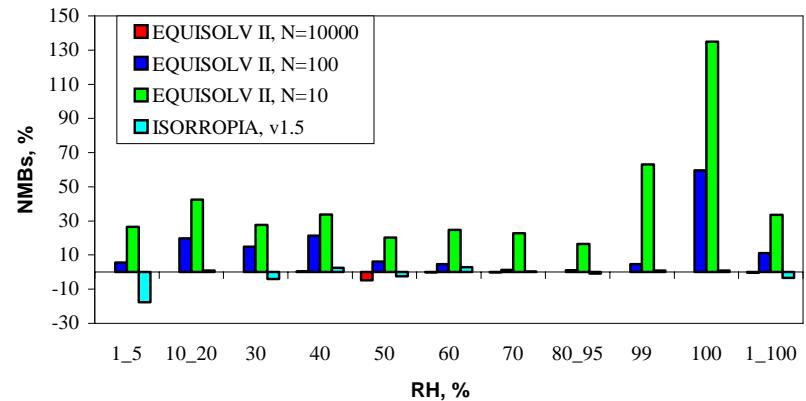
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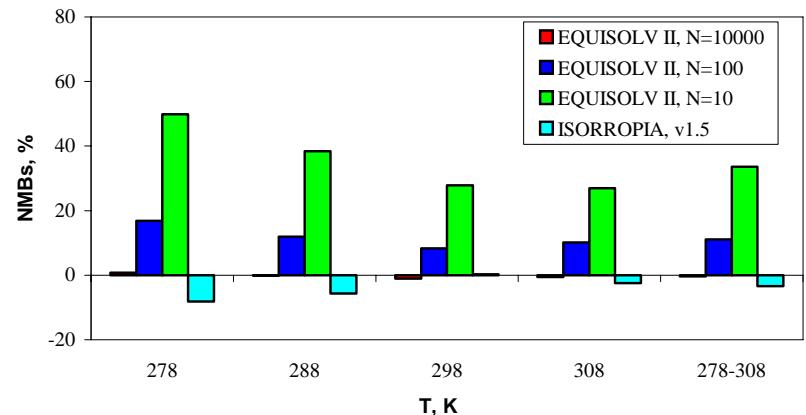
TSO4 = 20



NMBs for NH<sub>3</sub>(g) at T = 278-308 K, RH = 1-100%, and [TSO4]=5, 20 l g m<sup>-3</sup>

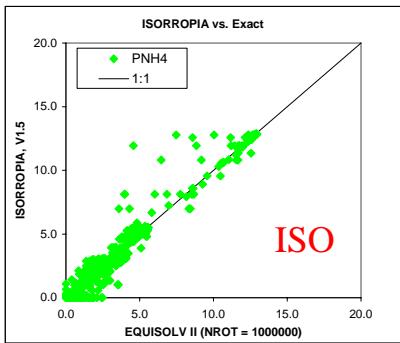


NMBs for NH<sub>3</sub>(g) at T = 278-308 K, RH = 1-100%, and [TSO4]=5, 20 l g m<sup>-3</sup>

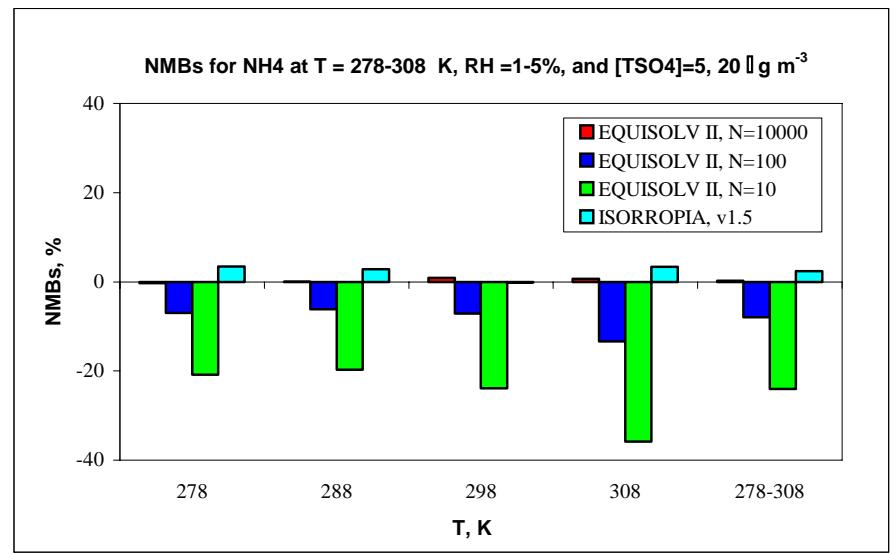
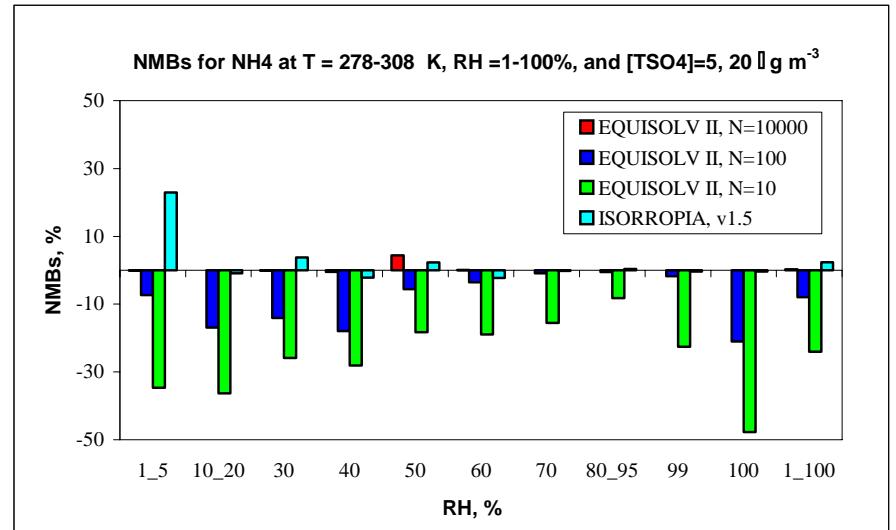
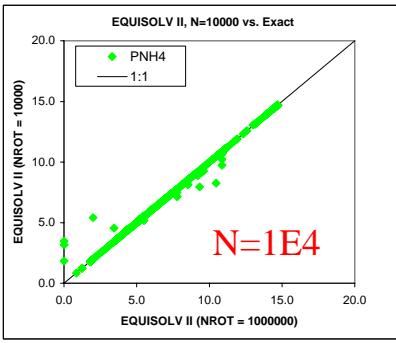
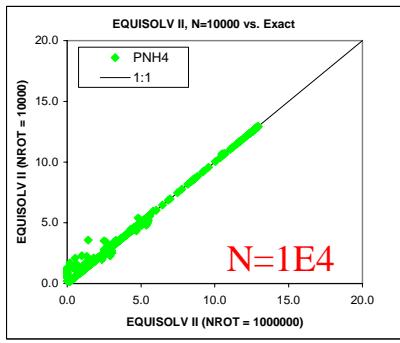
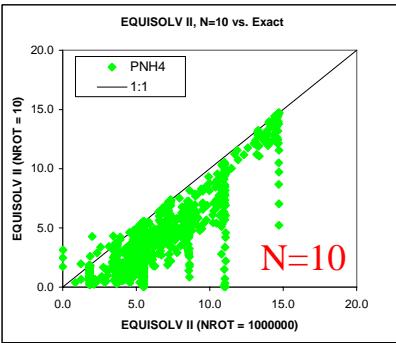
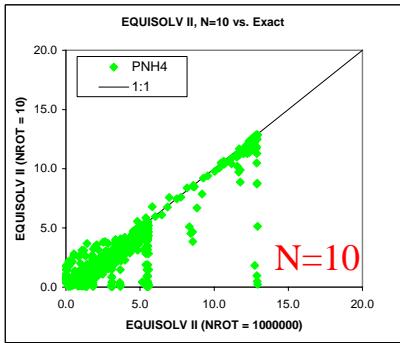
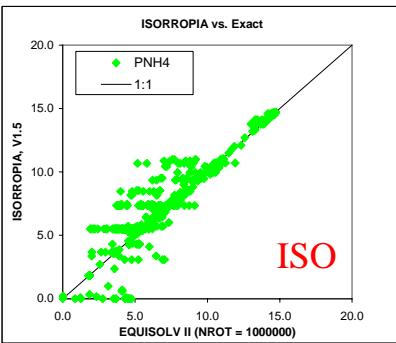


# Box Model Results: NH<sub>4</sub><sup>+</sup>

TSO4 = 5

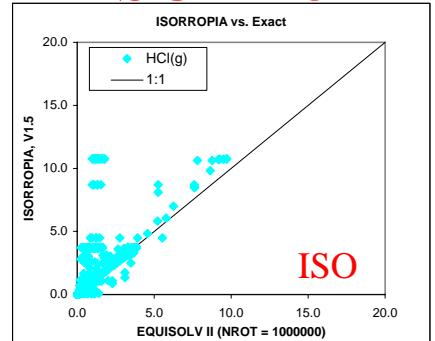


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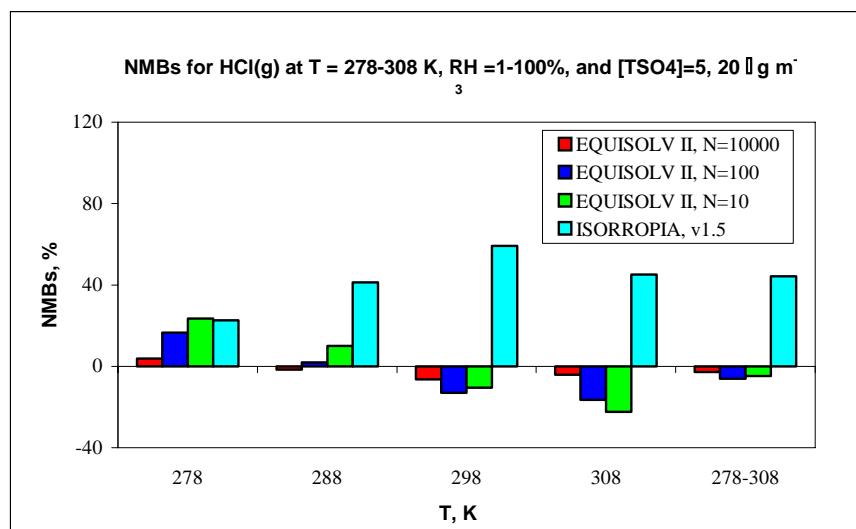
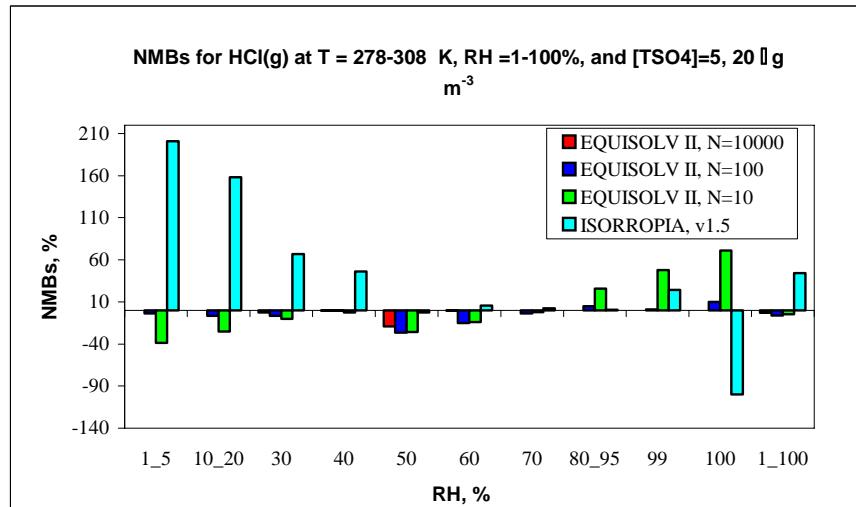
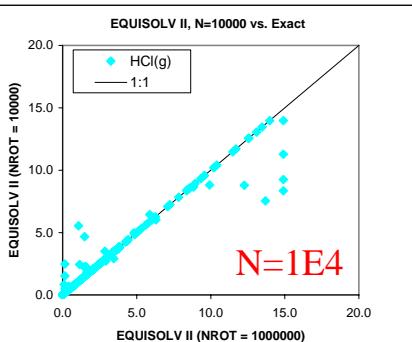
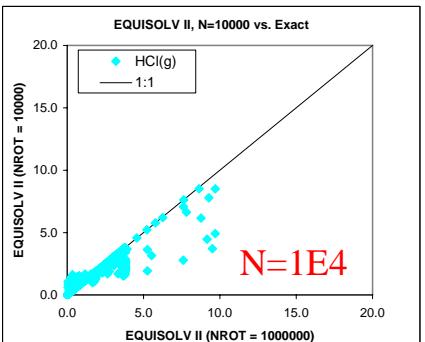
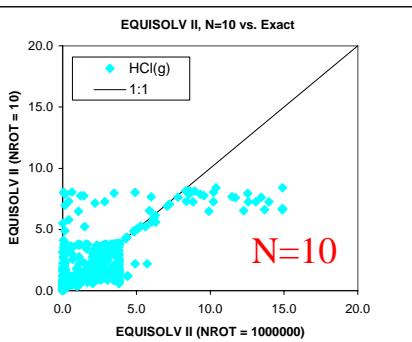
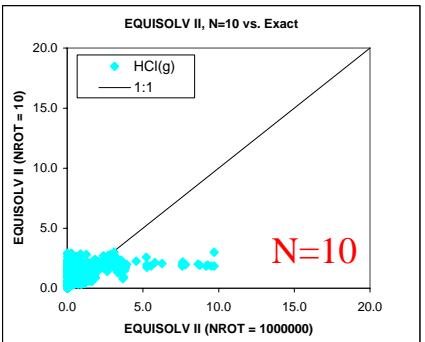
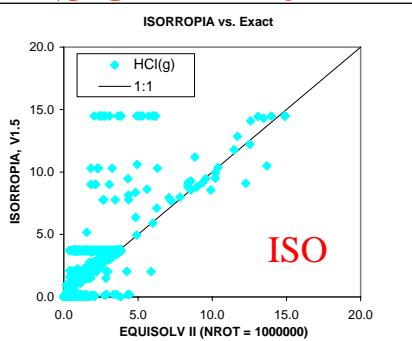


# Box Model Results: HCl(g)

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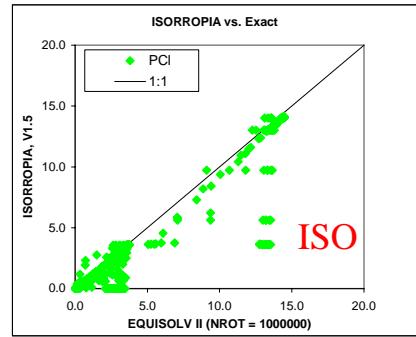


**TSO4 = 20**

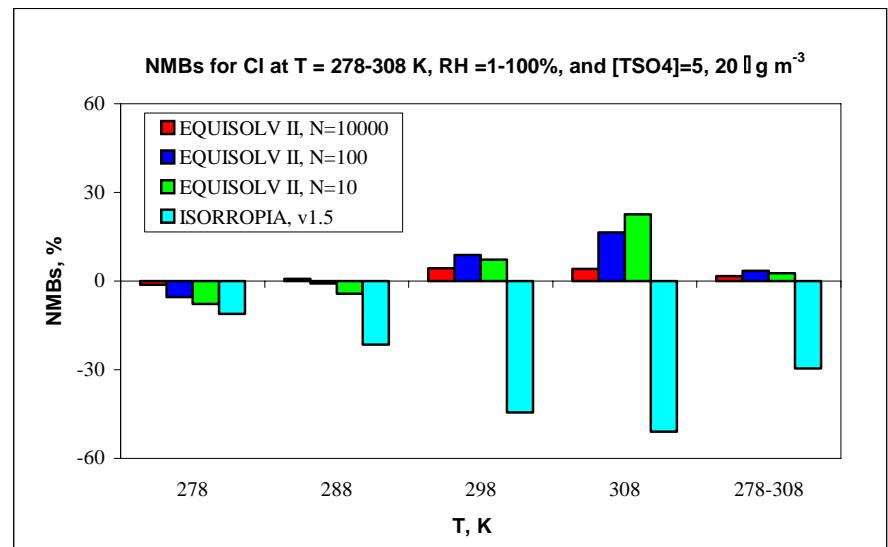
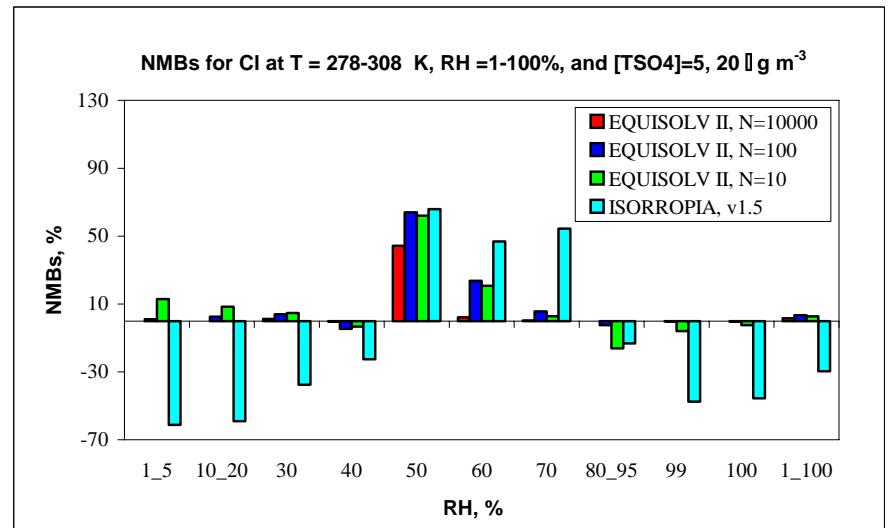
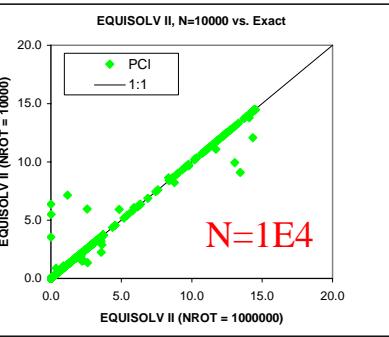
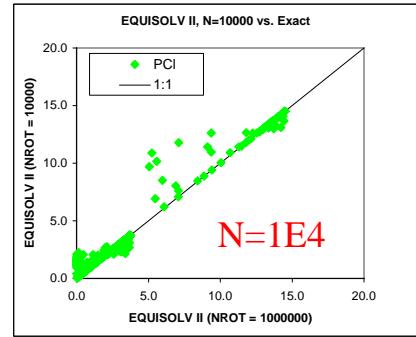
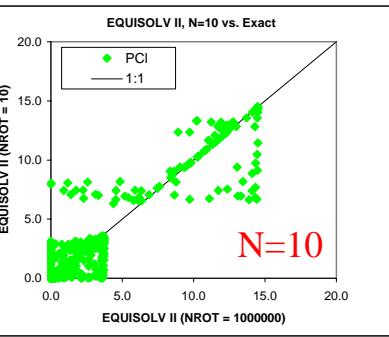
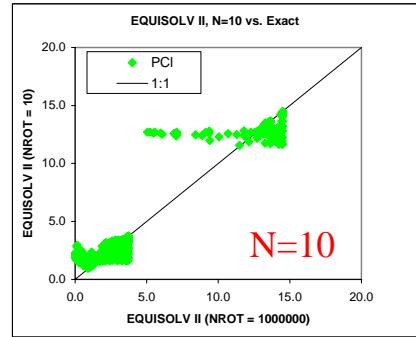
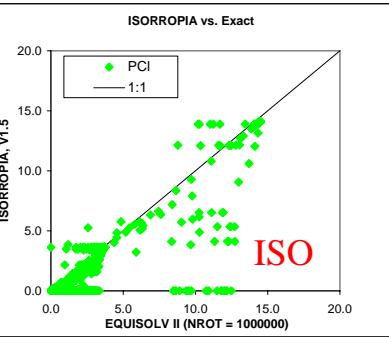


# Box Model Results: Cl-

**TSO4 = 5**



**TSO4 = 20**



# Differences in Equilibrium Reactions

## EQUISOLV II

1.  $NH_3(g) + H^+ \rightleftharpoons NH_4^+$
2.  $NH_3(g) + HNO_3(g) \rightleftharpoons NH_4^+ + NO_3^-$
3.  $NH_4Cl(s) \rightleftharpoons NH_4^+ + Cl^-$
4.  $NH_4NO_3(s) \rightleftharpoons NH_4^+ + NO_3^-$
5.  $HNO_3(g) \rightleftharpoons HNO_3(l)$
6.  $H_2SO_4(l) \rightleftharpoons H^+ + HSO_4^-$

} → Gives lower  $HNO_3(g)/NH_4^+$ ;  
higher  $NO_3^-/NH_3(g)/Cl^-$

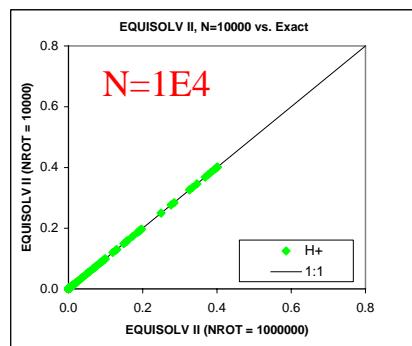
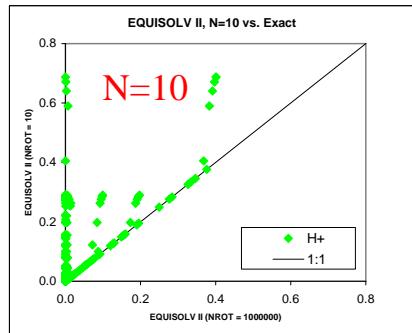
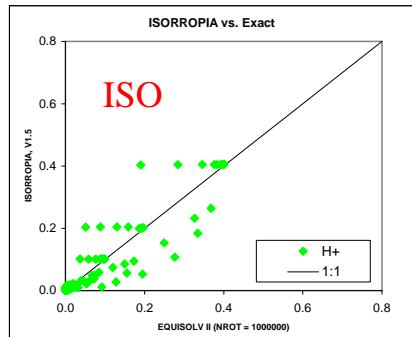
## ISORROPIA

7.  $NH_3(g) + H_2O \rightleftharpoons NH_4^+ + OH^-$
8.  $NH_4Cl(s) \rightleftharpoons NH_3(g) + HCl(g)$
9.  $NH_4NO_3(s) \rightleftharpoons NH_3(g) + HNO_3(g)$

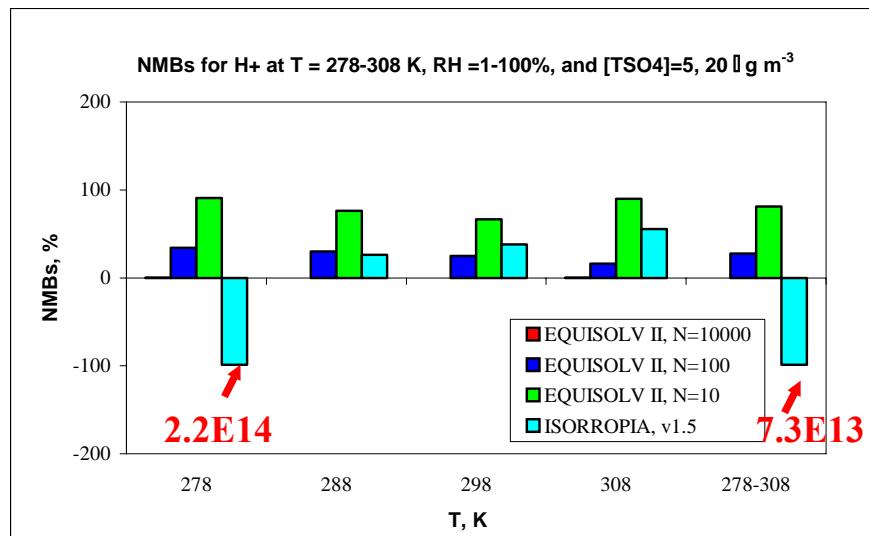
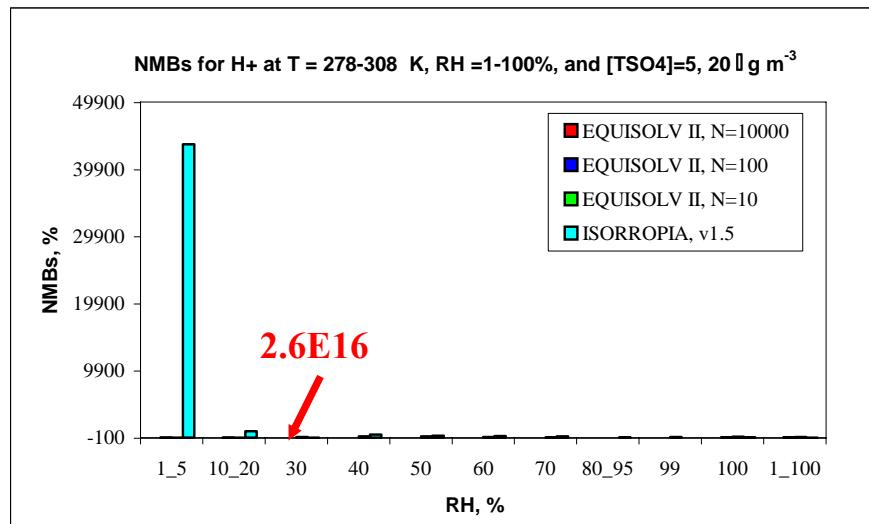
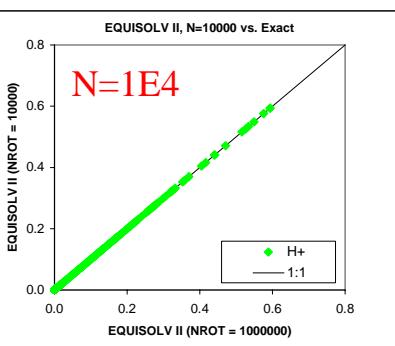
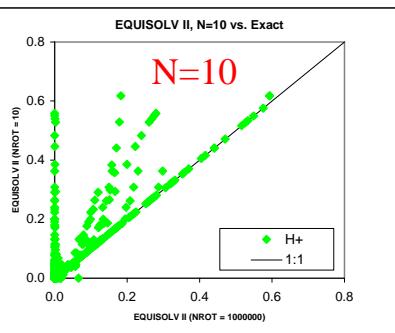
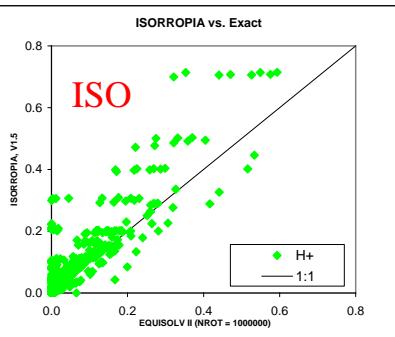
} → Gives higher  $HNO_3(g)/NH_4^+$ /  
 $HCl(g)$ ; lower  $NO_3^-/NH_3(g)$

# Box Model Results: H<sup>+</sup>

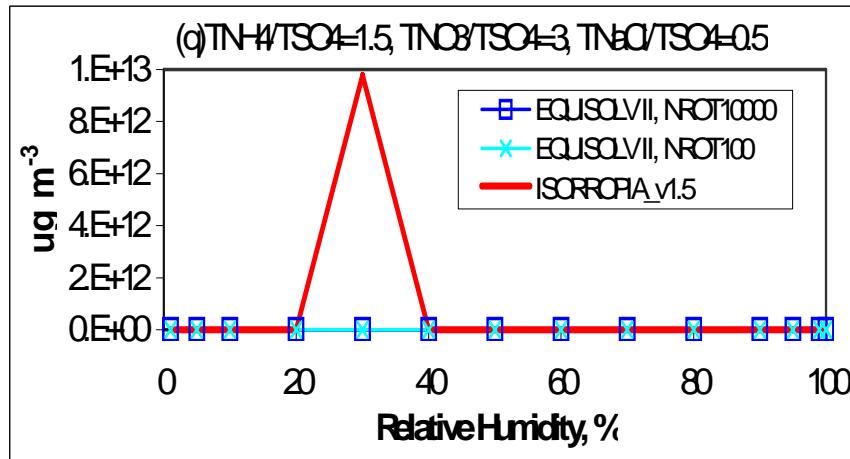
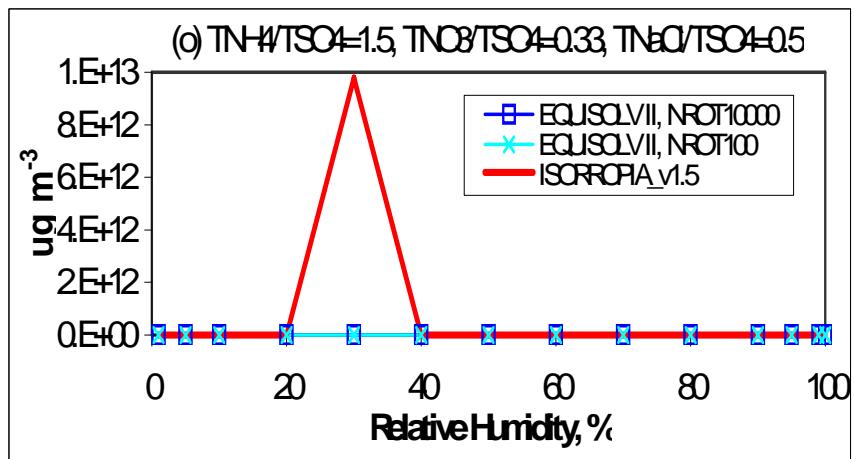
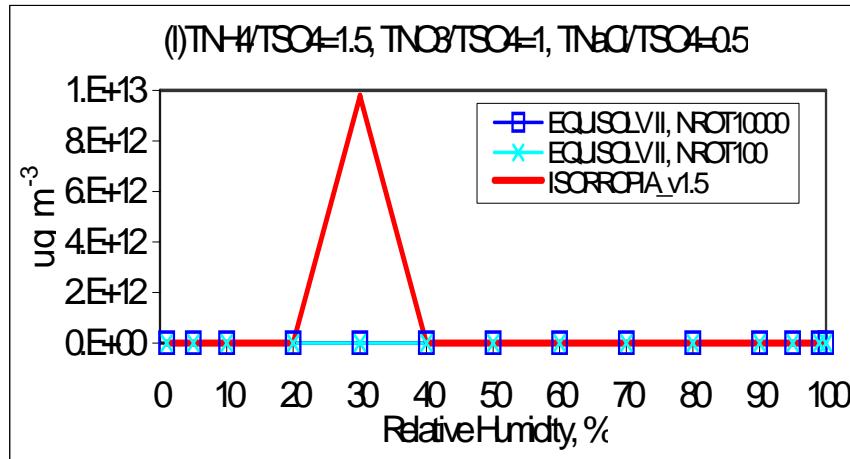
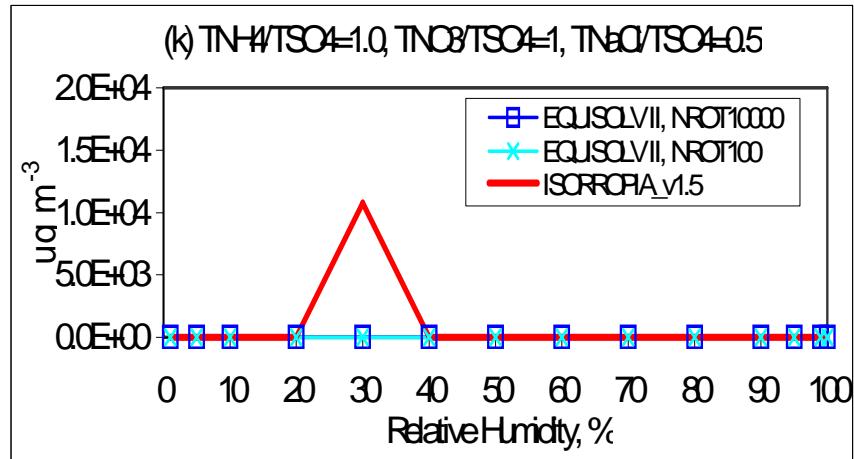
**TSO4 = 5**



**TSO4 = 20**

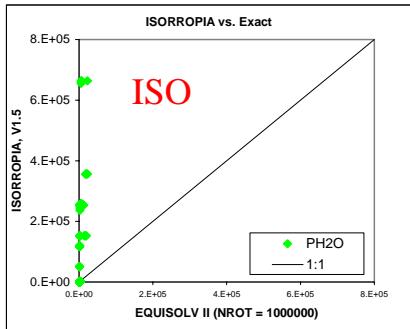


# Predicted $[H^+]$ at $T = 278$ K, $TSO_4 = 20 \mu\text{g m}^{-3}$

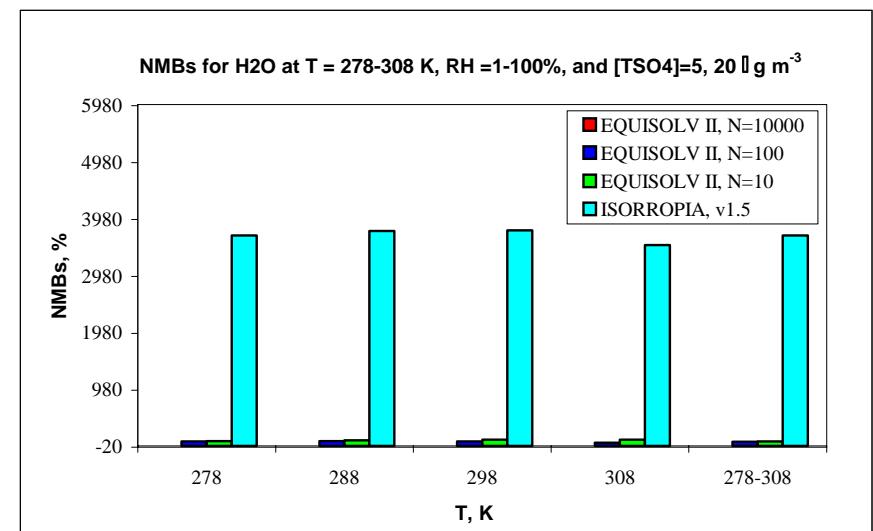
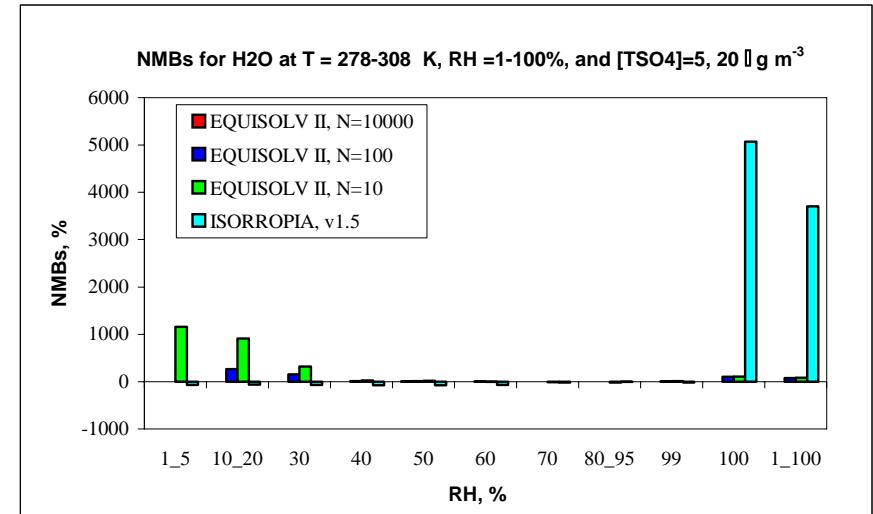
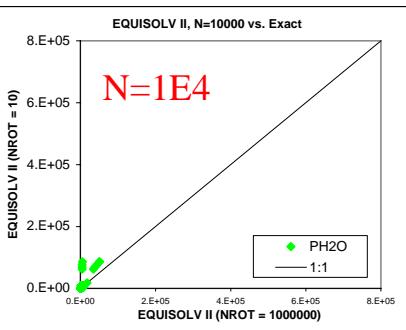
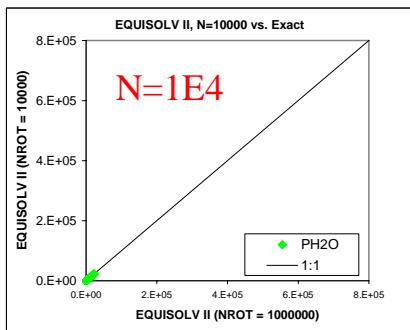
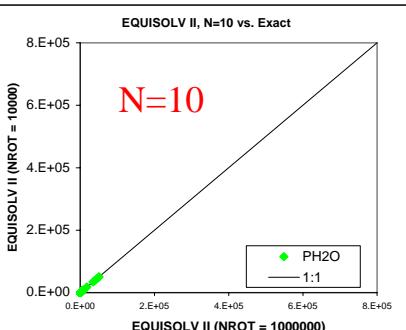
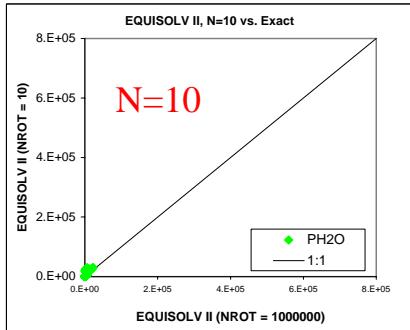
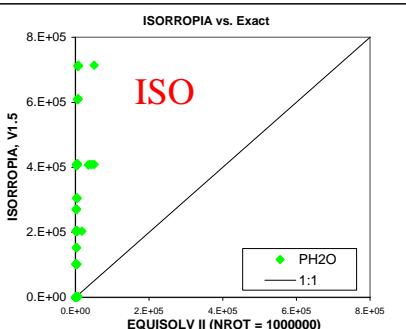


# Box Model Results: H<sub>2</sub>O

**TSO4 = 5**



**TSO4 = 20**



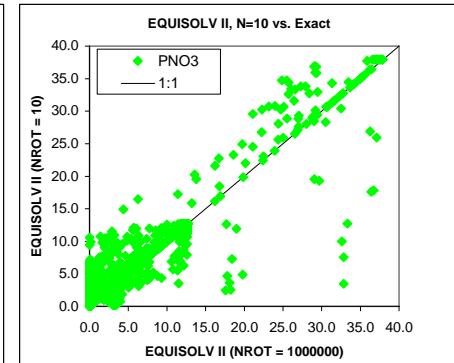
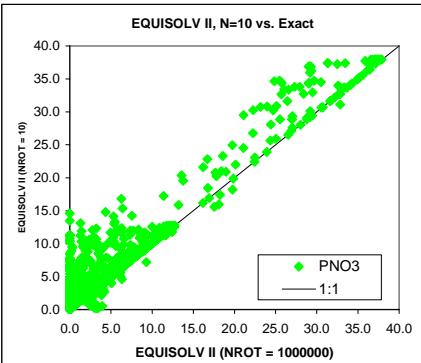
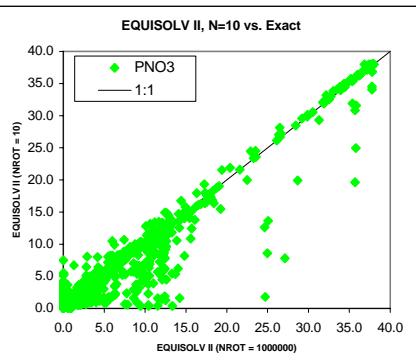
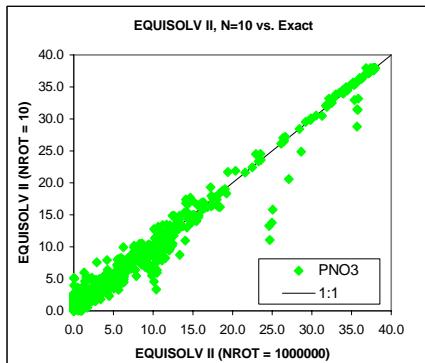
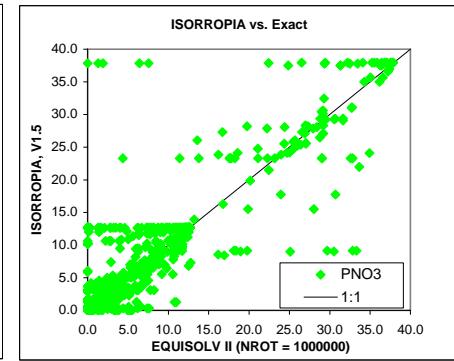
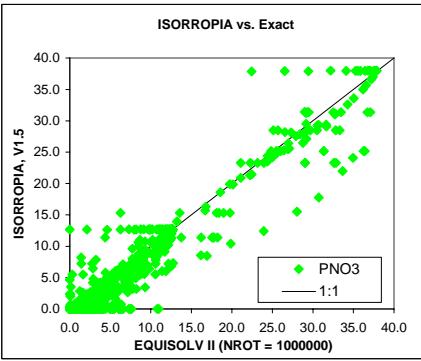
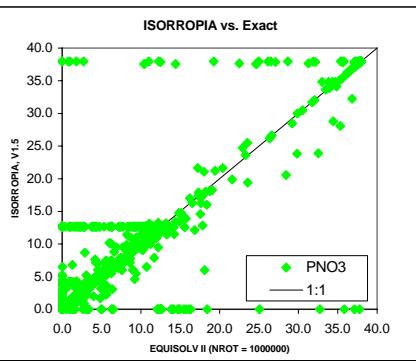
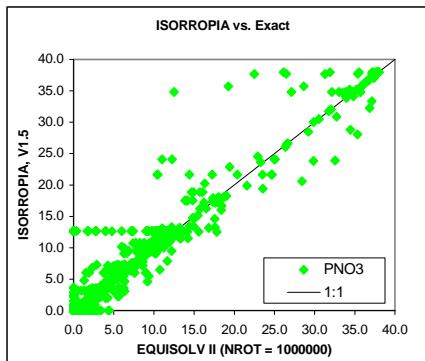
# Box Model Results: Predictions of $\text{NO}_3^-$

## Solid + Liquid vs. Liquid only

$\text{TSO}_4 = 5$

Solid+Liquid

Liquid



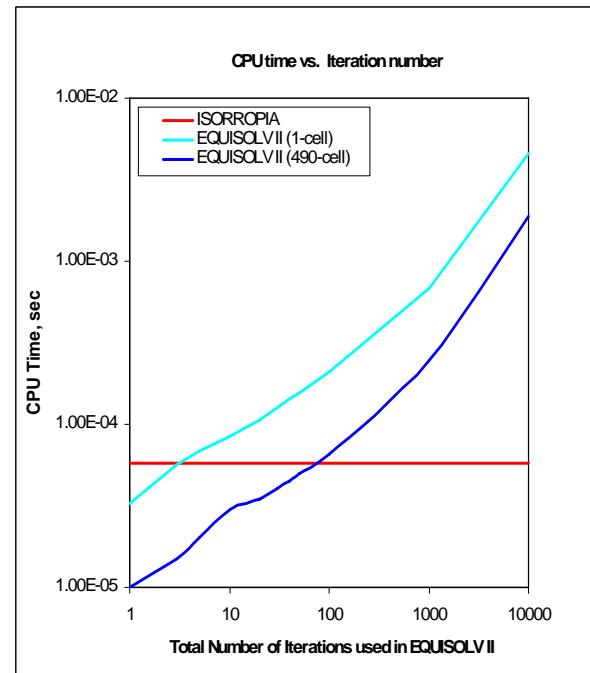
Top: ISORROPIA vs. Exact

Bottom: EQUISOLV II, NROT = 10 vs. Exact

# Box Model: Timing Test

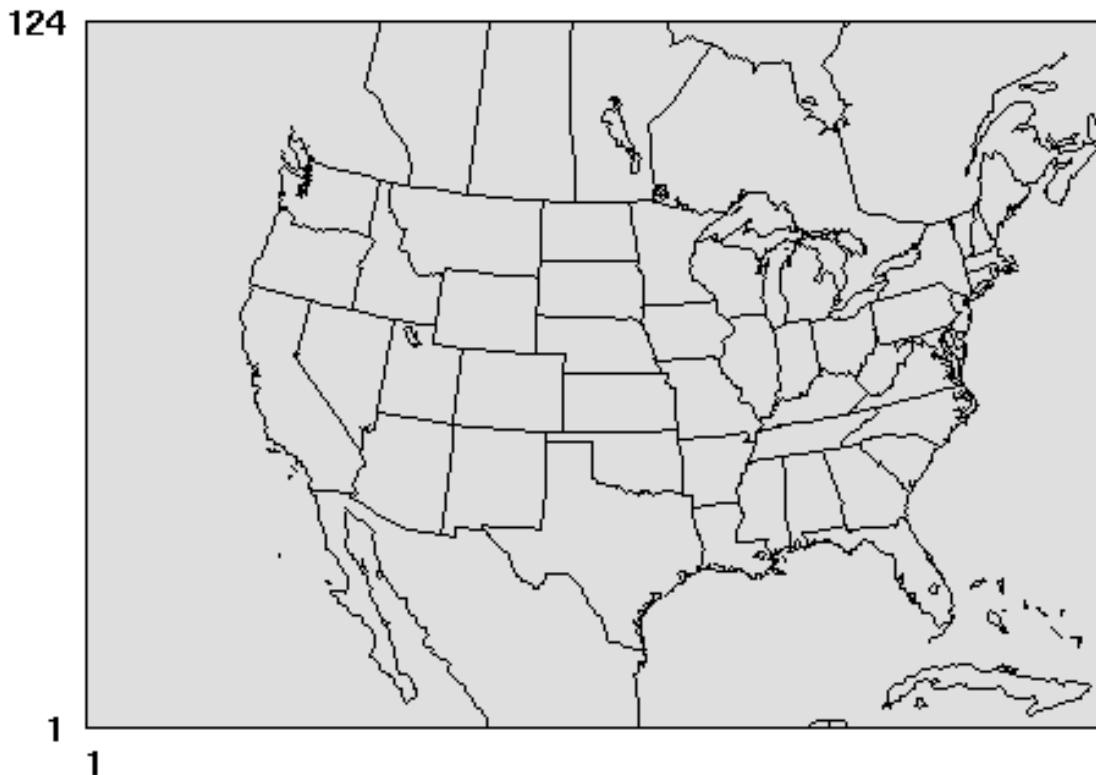
280 Cases with T=298 K, RH=1-100%, TSO4= 20  $\mu\text{g m}^{-3}$

ISORROPIA		EQUISOLV II		
Iteration Numbers	CPU Time, s	NROT	CPU Time, s (Single-cell)	CPU Time, s (490-cell)
MAXIT=100 NSWEEPI=4	$5.77 \times 10^{-5}$	1	$2.97 \times 10^{-5}$	$1.00 \times 10^{-5}$
		3	$5.36 \times 10^{-5}$	$1.50 \times 10^{-5}$
		5	$6.49 \times 10^{-5}$	$2.00 \times 10^{-5}$
		10	$8.06 \times 10^{-5}$	$3.00 \times 10^{-5}$
		20	$1.03 \times 10^{-4}$	$3.51 \times 10^{-5}$
		30	$1.21 \times 10^{-4}$	$4.01 \times 10^{-5}$
		40	$1.35 \times 10^{-4}$	$4.49 \times 10^{-5}$
		50	$1.51 \times 10^{-4}$	$5.03 \times 10^{-5}$
		100	$2.02 \times 10^{-4}$	$6.49 \times 10^{-5}$
		1000	$6.74 \times 10^{-4}$	$2.50 \times 10^{-4}$
		10000	$4.34 \times 10^{-3}$	$1.89 \times 10^{-3}$



# 3-D Test with CMAQ for the June 1999 SOS Episode

- Simulation Period                    12-28 June 1999
- Grid Resolution                    32 km,  $178 \times 124$  grid cells, 19 layers
- Meteorology                        MM5/FDDA
- Emissions                            EPA's NEI'99 inventory
- Initial/Boundary cond.            2-day spinup, CMAQ default ICs/BCs
- CMAQ                                V 4.4, SAPRC99/EBI or ROS3, modified to include ternary nucleation



## Datasets for Evaluation

**CASTNet:** hourly  $O_3$ , weekly  $SO_4^{2-}$ ,  $NO_3^-$ ,  $NH_4^+$  at 83 sites

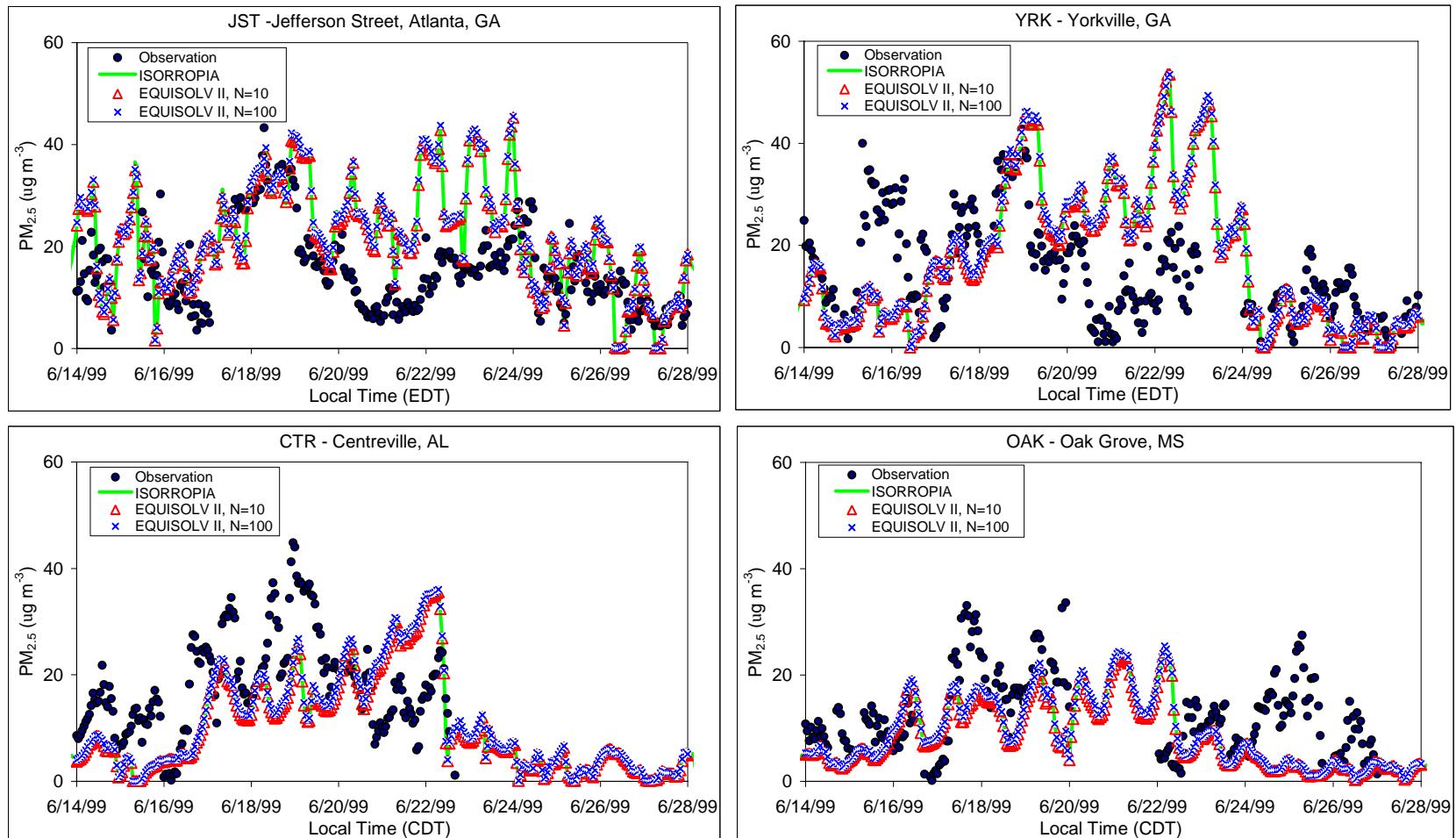
**IMPROVE:** 3-day  $SO_4^{2-}$ ,  $NO_3^-$ ,  $NH_4^+$ , EC, OC; 24-hr  $PM_{2.5}$  at 145 sites

**STN:** 3-day  $SO_4^{2-}$ ,  $NO_3^-$ ,  $NH_4^+$ , EC, OC,  $PM_{2.5}$  at 139 sites

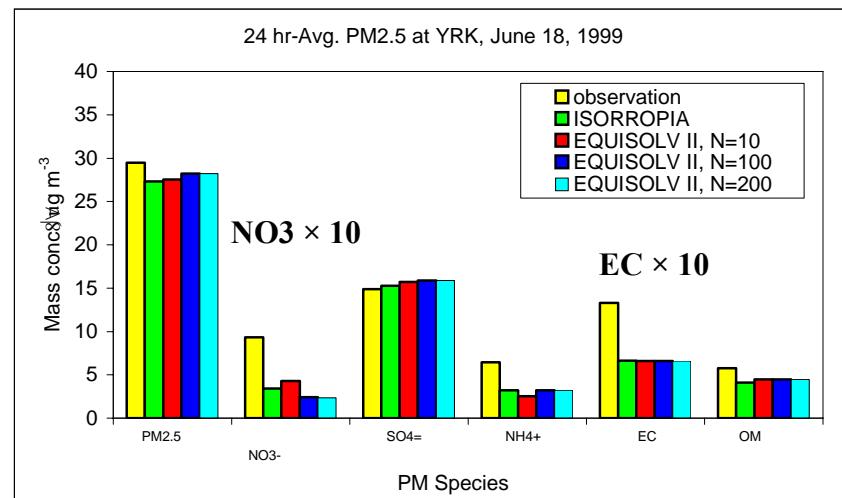
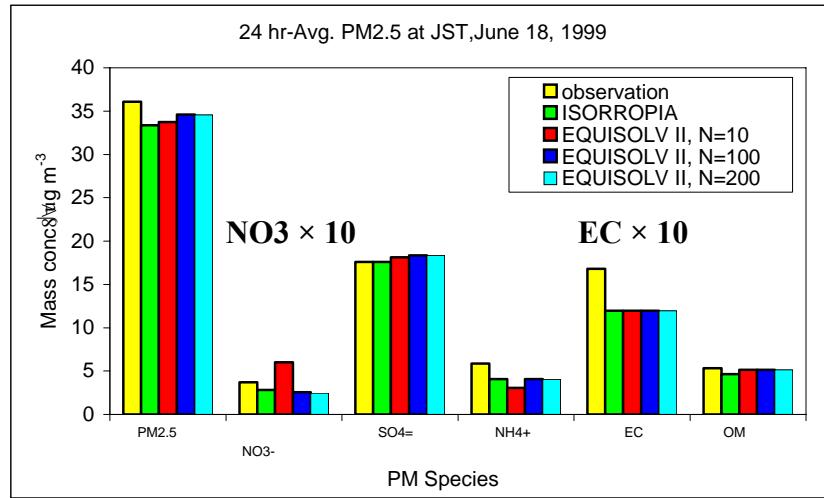
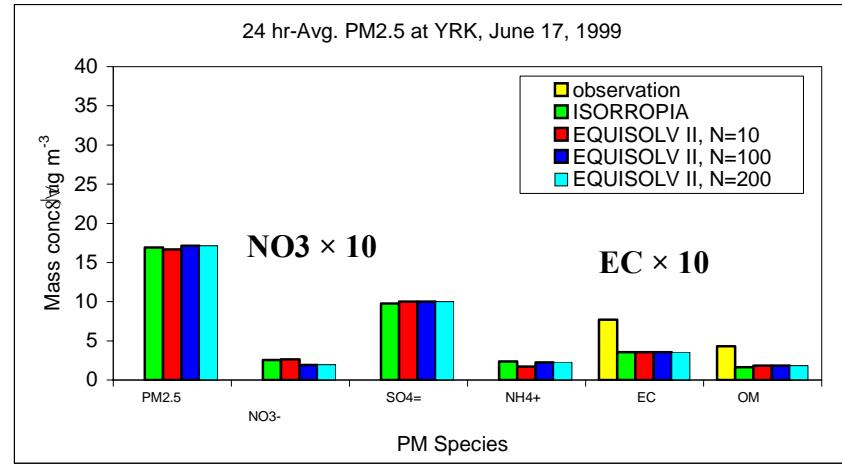
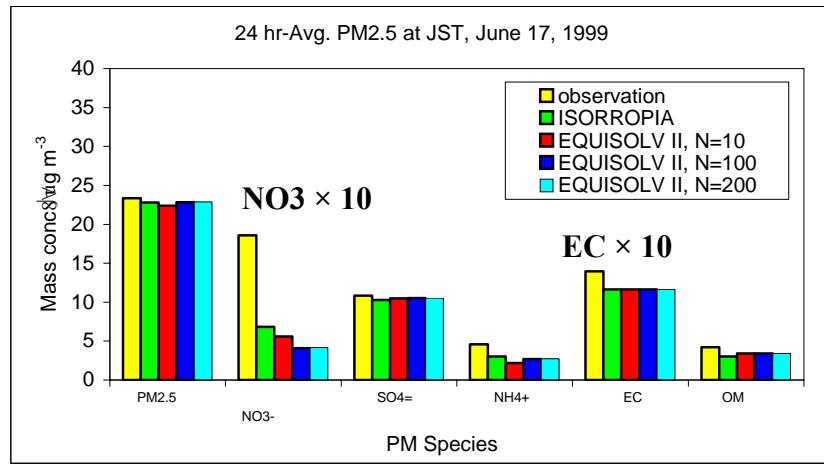
**AIRS:** hourly  $O_3$  at 1161 sites

**SEARCH:** Hourly  $O_3$ ; 24-hr  $PM_{2.5}$  at JST, YRK, BHM, CTR, OLF, PNS, OAK, GFP

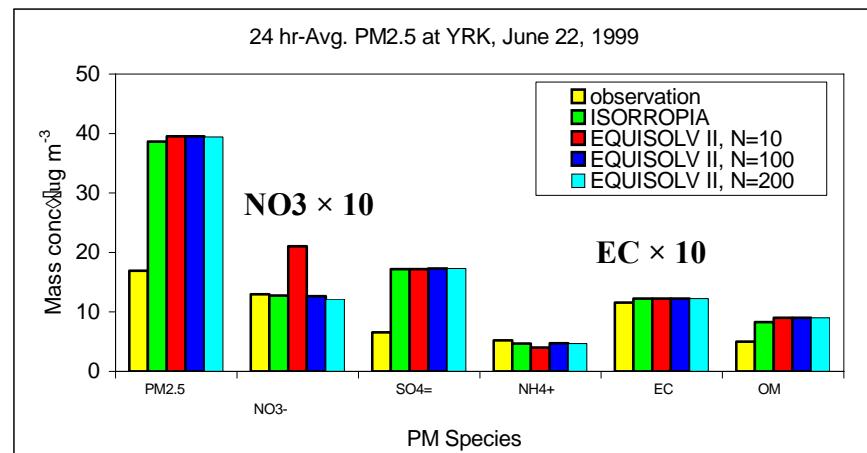
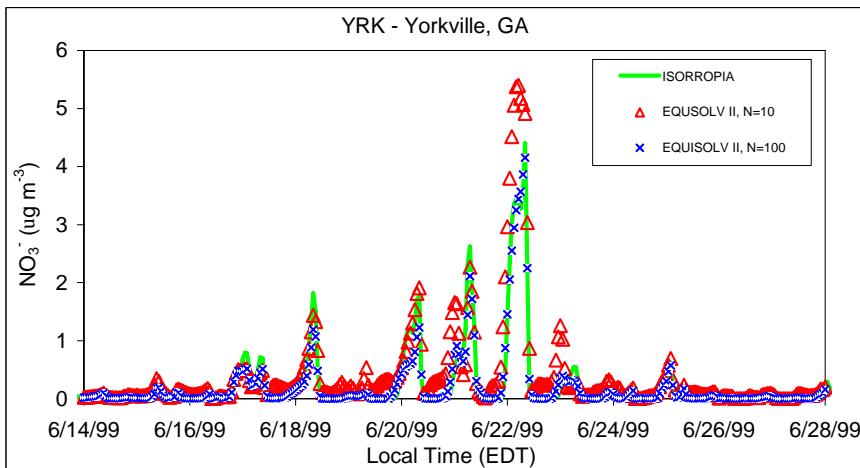
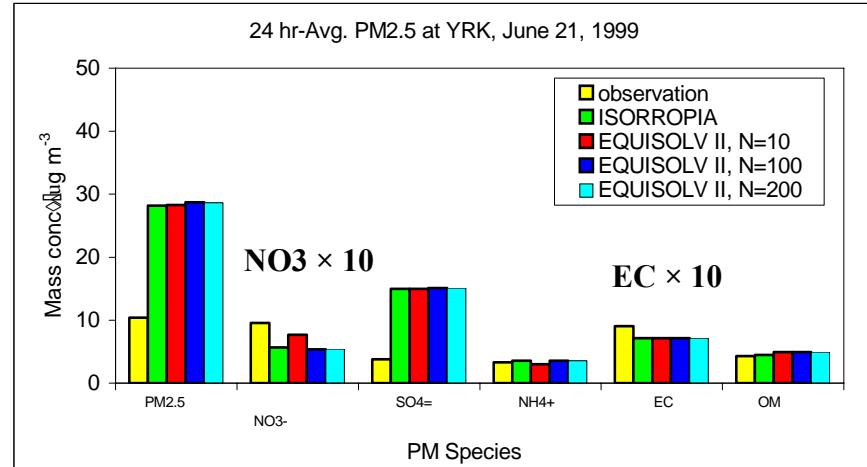
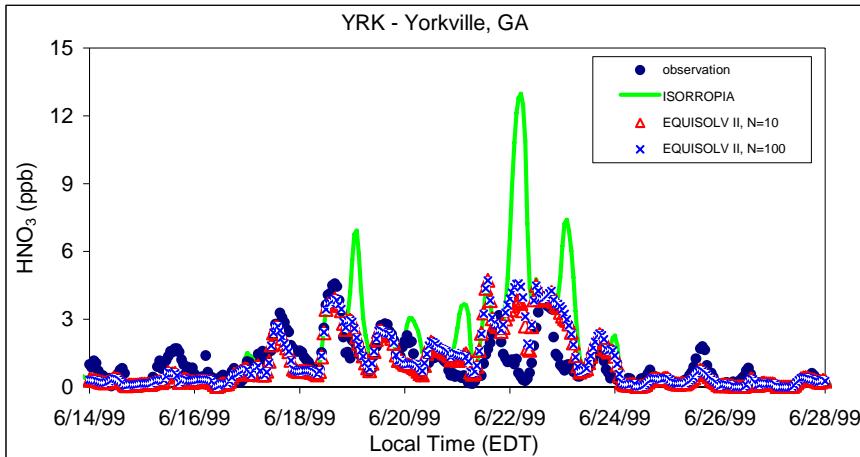
# Observed vs. Predicted PM<sub>2.5</sub> at SEARCH Sites



# Observed vs. Predicted PM<sub>2.5</sub> and Its Composition at JST and YRK, GA



# Observed vs. Predicted $\text{HNO}_3$ , $\text{NO}_3^-$ and $\text{PM}_{2.5}$ Composition at YRK, GA



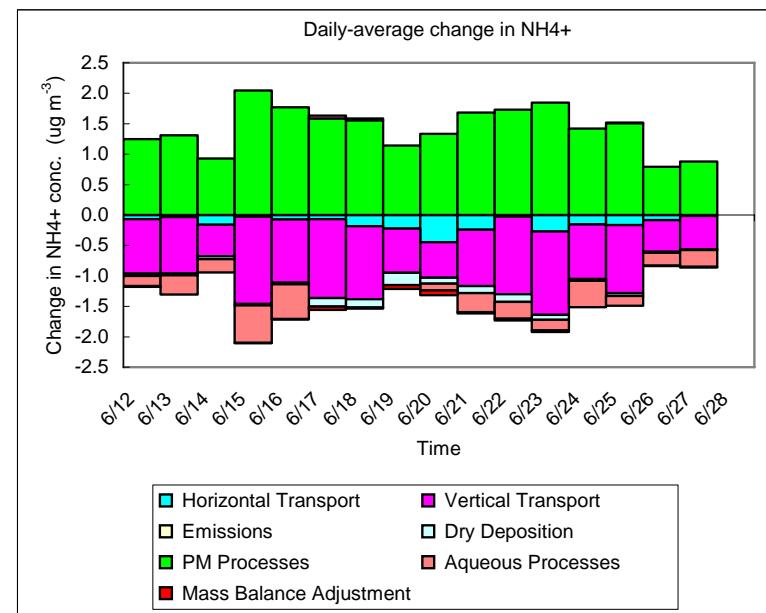
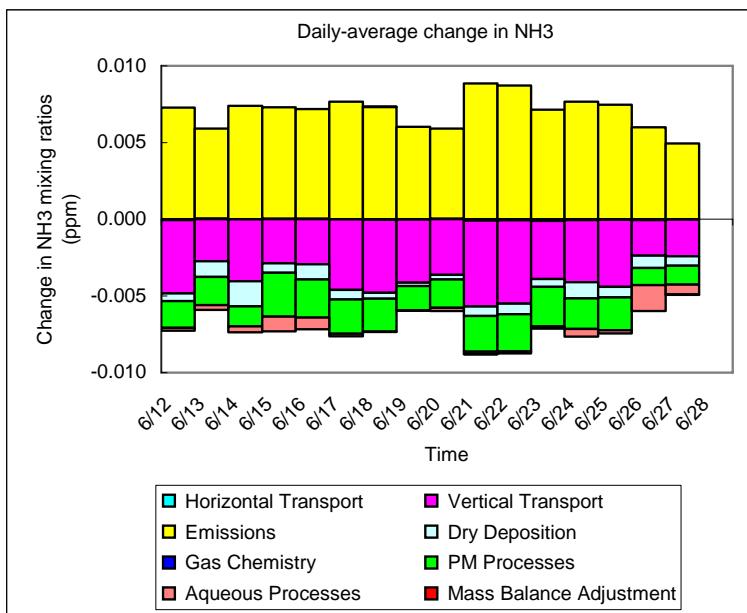
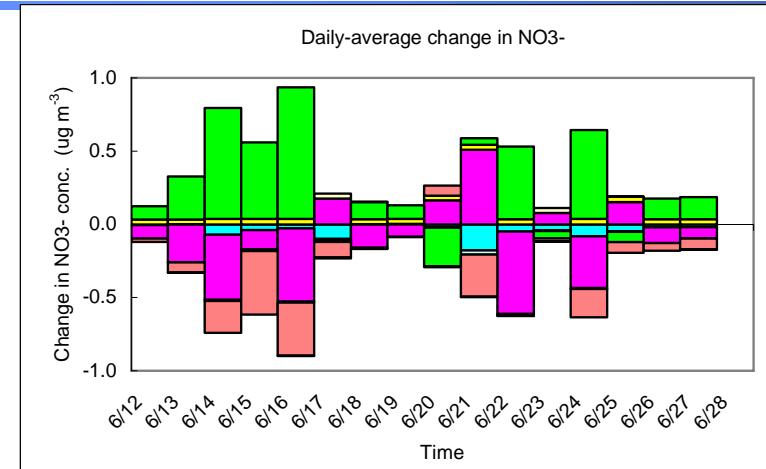
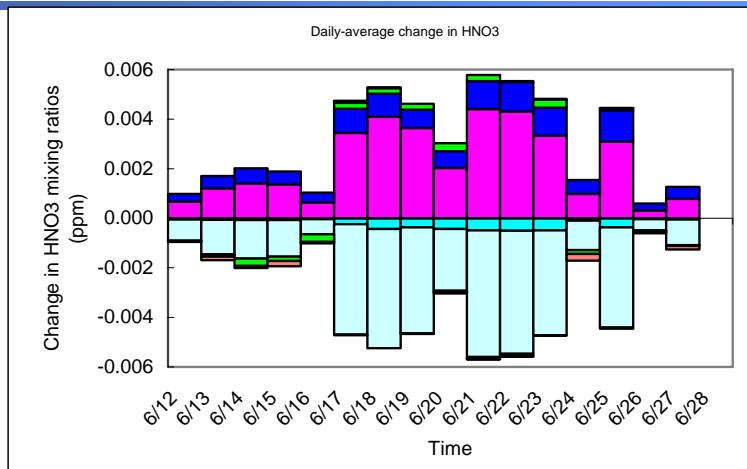
# ISORROPIA vs. EQUISOLV: Performance Statistics

Normalized Mean Error and Bias (Fraction)

Normalized Mean Error Factor and Bias Factor (Fraction)

	Module	CASTNet		IMPROVE		SEARCH	
		NME %	NMB %	NME %	NMB %	NME %	NMB %
<b>PM<sub>2.5</sub></b>	ISO			38	-26	42	-3
	EQUI			39	-29	42	-5
<b>Sulfate<sub>2.5</sub></b>	ISO	29	14	49	18	53	22
	EQUI	30	15	49	19	53	23
<b>Nitrate<sub>2.5</sub></b>	ISO	89	-16	96	-42	76	-71
	EQUI	75	-24	89	-49	67	-51
<b>Ammonium<sub>2.5</sub></b>	ISO	28	5	36	23	47	-32
	EQUI	41	-37	30	-22	63	-60
<b>BC<sub>2.5</sub></b>	ISO			47	-34	55	-53
	EQUI			47	-35	54	-51
<b>OC<sub>2.5</sub></b>	ISO			43	-25	41	-34
	EQUI			43	-25	41	-34

# Daily Average Changes in $\text{HNO}_3/\text{NO}_3^-$ and $\text{NH}_3/\text{NH}_4^+$ Due to Major Processes



# Summary

- EQUISOLV II ( $N \leq 10$ ) gives lower biases (< 10%) for  $\text{HNO}_3$ ,  $\text{NO}_3^-$ ,  $\text{HCl}$ ,  $\text{Cl}^-$ ,  $\text{SO}_4^{2-}$ ,  $\text{H}_2\text{O}$ ,  $\text{H}^+$ , and  $\text{NH}_3$  (except for  $\text{RH} \geq 99$ ) and moderate biases (~27%) for  $\text{NH}_4^+$ . ISORROPIA gives lower biases for  $\text{HNO}_3$ ,  $\text{NO}_3^-$ ,  $\text{SO}_4^{2-}$ ,  $\text{H}_2\text{O}$  (except  $\text{RH} = 100$ ),  $\text{H}^+$  (except  $\text{RH} \leq 5$ ),  $\text{NH}_3$  and  $\text{NH}_4^+$ ; moderate biases (~30-60%) for  $\text{HCl}$ ,  $\text{Cl}^-$  and abnormally high  $\text{H}_2\text{O}$  and  $\text{H}^+$  biases (> 4E3-2.6E14%) under some conditions. Larger biases occur for  $\text{RH} \leq 40$  or  $\geq 99$  for most species.
  - A thermodynamically metastable system (solid + liquid)
  - High sulfate conditions: ISORROPIA overestimates  $\text{HNO}_3(\text{g})$  and underestimates  $\text{NO}_3^-$ ; EQUISOLV II ( $N=10$ ) gives opposite trends.
  - A supersaturated system (no solid)
  - ISORROPIA gives some abnormally high or low  $\text{HNO}_3(\text{g})$  and  $\text{NO}_3^-$ ; EQUISOLV II with  $N \leq 100$  gives slightly worse results than the metastable system (solid+liquid).
- CMAQ with EQUISOLV II and ISORROPIA performs similarly except for  $\text{NO}_3^-$  and  $\text{NH}_4^+$ . EQUISOLV II (solid and liquid) gives better  $\text{NO}_3^-$  at SEARCH sites, ISORROPIA (no solid) gives slightly better  $\text{NO}_3^-$  for IMPROVE and CASTnet sites, but it gives  $[\text{HNO}_3]$  much higher than the observed one at some sites. Differences in  $\text{NO}_3^-$  and  $\text{NH}_4^+$  predictions can be explained by different reactions and the high  $\text{NO}_3^-$  predicted by ISORROPIA with liquid only. Thermodynamics only may not explain the observed gas/particle partitioning.
- Future work include multiple-cell implementation, size-resolved equilibrium, and application of CMAQ-EQUISOLV II for regions with crustal species and sea-salt.