# A Multiphase Adjoint Model for CMAQ

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## Outline

- Motivation for developing a multiphase adjoint model
- The current status of the development
  - Adjoint code
  - Process-by-process validation
  - Test run of the full adjoint model
- Concluding remarks

# Motivation

- CMAQ: Evolution of atmospheric gas and aerosol species
- Forward sensitivity analysis (Decoupled Direct Method, DDM)

#### source receptor





#### Forward

Backward

Backward/Adjoint sensitivity analysis

# Adjoint sensitivity analysis: An example

Pappin et al., "Compounding Benefits of Air Pollution Control: A Revised View of Air Pollution Economics", Wednesday Presentation

# Benefits-per-ton of NO<sub>x</sub> Control At 2007 Emission Levels



## The current status of the adjoint development

- CMAQ scientific processes: chemistry, aerosol, transport, cloud
- Adjoint code generated by tools (KPP, Tapenade, TAMC) or by hand
- Code validating using
  - Finite Difference Method (FDM)

$$f'(x) = \frac{f_{x+h} - f_{x-h}}{2h} + O(h^2)$$

• Complex Variable Method (CVM)

$$f(x) = \frac{\Im (f(x+ih))}{h} + O(h^2)$$

and sometimes DDM/TLM

# Process-by-process validation

Process	Sub-processes	Validation Methods
Chemistry		Finite difference Complex variable
Aerosol	Secondary organic aerosol, Heterogeneous chemistry, Coagulation, Nucleation, Condensation, Thermodynamics (Isorropia; Capps et al., 2012)	Finite difference Complex variable
Transport	Horizontal/vertical advection, Horizontal/ vertical diffusion	Finite difference
Cloud	Convective cloud, Resolved cloud, Aqueous chemistry	Finite difference Complex variable Tangent linear model

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# Th adjoint of chemistry: Limitations of the FDM





### Finite difference $\frac{\partial O3}{\partial HCL}$



# The adjoint of chemistry

#### Adjoint



### Complex variable





# The adjoint of chemistry: Full Jacobian

Adjoint

#### Complex variable





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## The adjoint of aerosol: secondary organic aerosol



Adjoint

## The adjoint of aerosol: heterogeneous chemistry



## The adjoint of aerosol: coagulation



## The adjoint of aerosol dynamics

 $\frac{\partial PM_{2.5}}{\partial ANH4J}$ 



Adjoint

#### Complex variable

## The adjoint of aerosol: Isorropia

# **ANISORROPIA Evaluation**



across an atmospherically relevant range of concentrations 268-308 K

Capps, Henze, Hakami, Russell, and Nenes, ACP. 2012

# The adjoint of aerosol: aerosol dynamics and thermodynamics

 $\frac{\partial PM_{2.5}}{\partial ASO4J}$ 



Adjoint

#### Finite difference

# The adjoint of aerosol: aerosol dynamics and thermodynamics



Adjoint

#### Finite difference

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The adjoint of transport: horizontal advection

• Horizontal advection at the X direction / discrete adjoint



## The adjoint of transport: vertical diffusion

 $\frac{\partial O3}{\partial O3}$ 



FDM

Adjoint

#### Finite Difference

## The adjoint of vertical diffusion and chemistry



Finite Difference

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## The adjoint of clouds

• Aqueous chemistry (KPP; Kathleen Fahey, EPA)

#### Adjoint

#### DDM



## Test run of the full adjoint model



## Test run of the full adjoint model





Day 4 without *AQCHEM* 



 $\frac{\partial PM_{2.5}}{\partial ASO4J}$ 

## Lessons learned

- Automatic differentiation entails a number of problems
  - Significant clean-up debugging is necessary
  - Single/double precision
  - Active variables passed by modules not visible to some top routines
  - Uninitialized variables in the adjoint code
- Problems that can be ignored in process-by-process tests may become more serious in interaction with other processes
- A number of issue can be avoided if forward model development is mindful of differentiation
  - Fractured response surface for a number of processes

## Concluding remarks

- When testing with the full adjoint model, blow-ups in the adjoint sensitivities caused by various reasons have been observed. Despite numerous bug fixes, large numbers still exist.
- Process-by-process validations are positive in general. But there seems to be interactions between processes which cause the abnormal growth in sensitivities.

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