



Statistical Comparison of Observed and Multi-Resolution CMAQ Modeled Hourly Ozone Concentration

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Abstract

CMAQ usually runs at multiple resolutions for research and policy purposes. This presentation compares observed hourly ozone concentrations to the CMAQ modeled hourly ozone concentrations at different spatial resolutions in Chicago area and in Atlanta area. Fractional bias (FB) and root normalized mean squared error (RNMSE) are calculated. The results show that high resolution CMAQ model output does not necessarily provide smaller FB and RNMSE than lower resolution runs. However, when high resolution output is aggregated to reduce small scale spatial fluctuations, one generally obtains better agreement than either the unaggregated high resolution model output or the low resolution model output in terms of RNMSE. We also decompose the total variation into components depending on hour, day and location and their interactions to better understand the statistical behavior of CMAQ model output at different resolutions. The temporal variation is captured reasonably well by CMAQ model output, but spatial variation and space-time interactions are not.

1 Case Study One: Chicago Area

1.1 Data

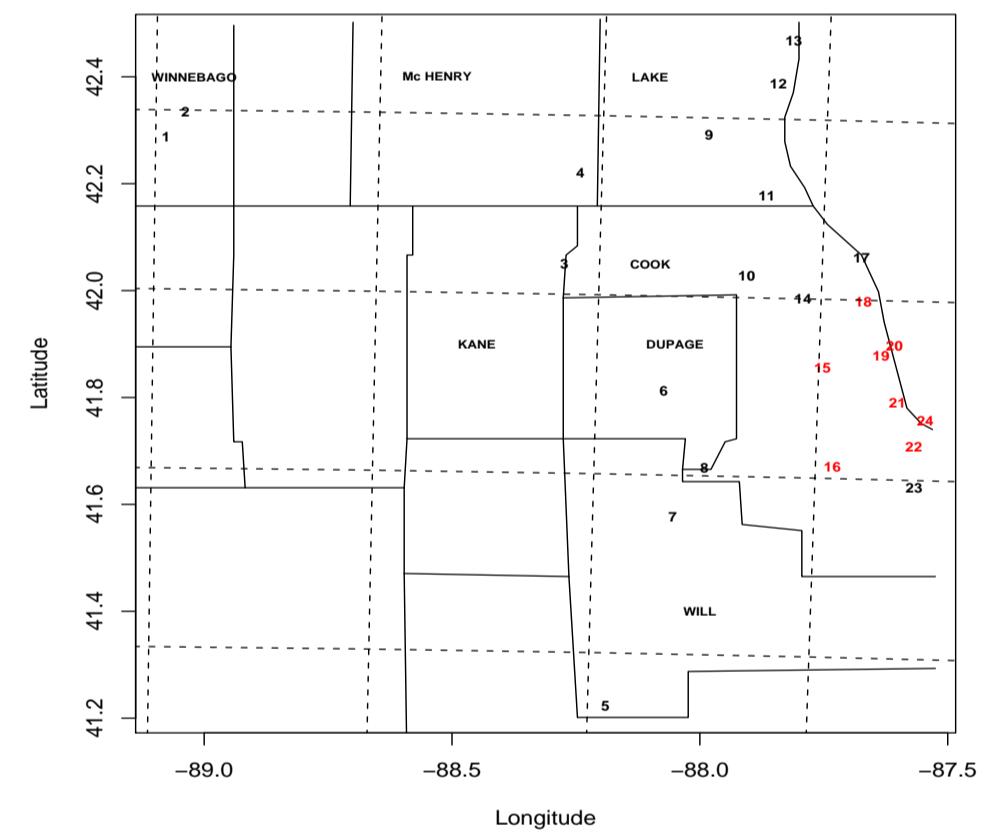


Figure 1: The Chicago area.

- Two sets of nested 36km, 12km and 4km CMAQ model output: one with low PBL input and the other with high PBL input.
- Observations at 24 monitoring sites.
- Time period: 06/24/1996 - 08/01/1996.
- Two regions: the Urban Region (the 36 km grid cell which contains monitors in red) and the Rural Region (everywhere else).

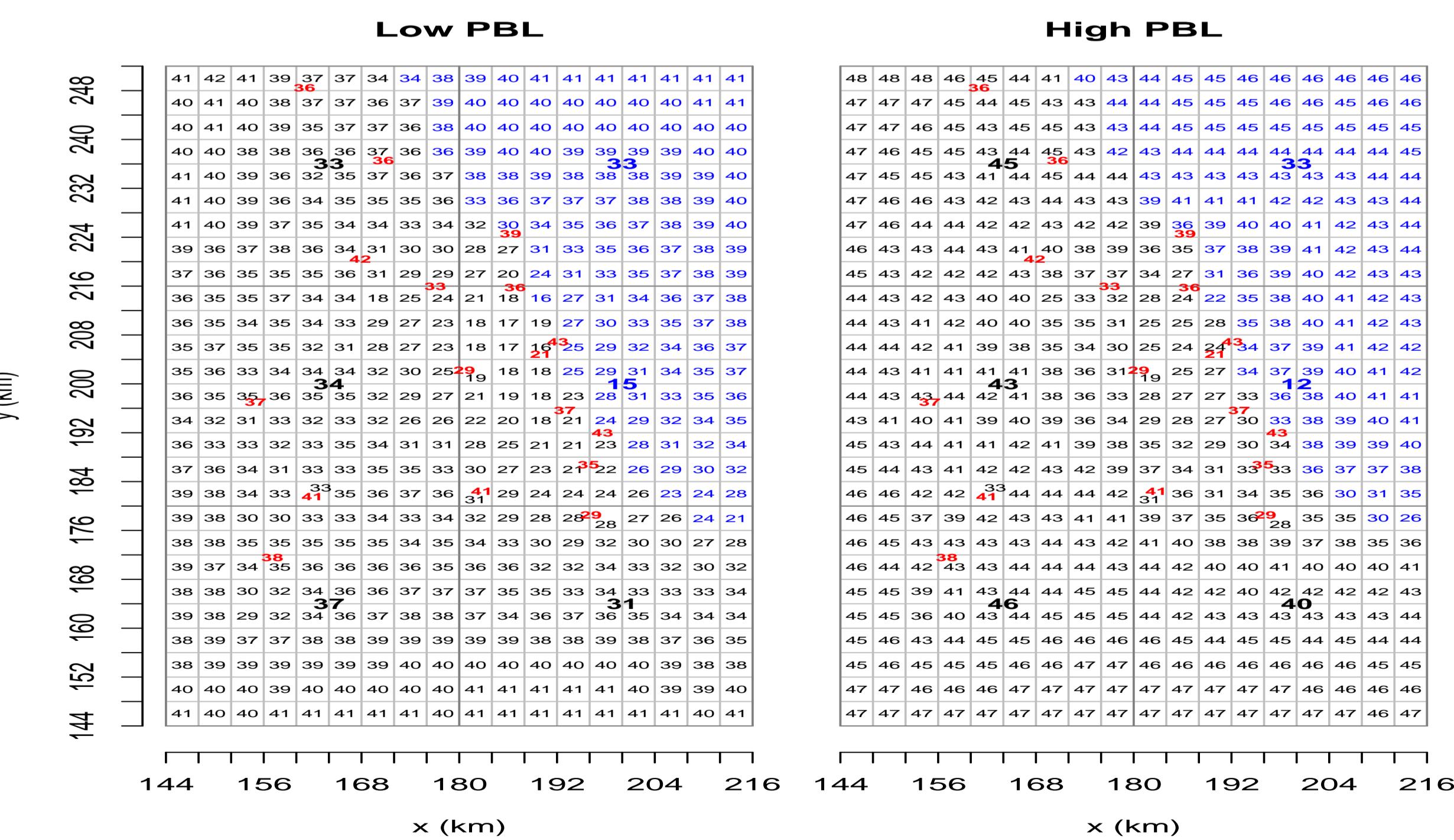


Figure 2: Day time average hourly ozone concentration (ppb).

1.2 FB and RNMSE

Write X_{ijk} the observed ozone at location i hour k on day j . Similarly, M_{ijk} is the model output from some version of the CMAQ model at location i hour k on day j (Shao et al. 2005). FB and

RNMSE (Canepa and Irwin 2005) are defined as

$$FB_i = \frac{\bar{M}_{i..} - \bar{X}_{i..}}{(\bar{M}_{i..} + \bar{X}_{i..})/2},$$

$$RNMSE_i = \sqrt{\frac{\frac{1}{N_i} \sum_{j,k} (M_{ijk} - X_{ijk})^2}{\bar{M}_{i..} \bar{X}_{i..}}},$$

where $\bar{M}_{i..} = \frac{1}{N_i} \sum_{j,k} M_{ijk}$, $\bar{X}_{i..} = \frac{1}{N_i} \sum_{j,k} X_{ijk}$, and N_i is the total number of non-missing observations at location i . The missing observations and the corresponding model output are not included in this step.

Table 1. FB and RNMSE for the Chicago area study ($\times 10^{-2}$).

	FB				RNMSE					
	M^{36}	M^{12}	A^{12}	M^4	A^4	M^{36}	M^{12}	A^{12}	M^4	A^4
RL	3	1	9	5	7	53	56	51	58	50
RH	20	20	25	14	23	52	53	51	53	50
UL	-27	-40	-9	-54	-8	89	93	69	109	68
UH	-27	-14	11	-24	10	91	73	62	81	61

1.3 Analysis of variance (ANOVA)

Let Z be a general notation for the quantity of interest. We decompose Z_{ijk} as,

$$Z_{ijk} = \mu + \alpha_i + \beta_j + \gamma_k + (\alpha\beta)_{ij} + (\alpha\gamma)_{ik} + (\beta\gamma)_{jk} + r_{ijk}. \quad (1)$$

- Every term sums to 0 when summed over any index, for example, $\sum_i (\alpha\beta)_{ij} = 0$ for all j and $\sum_j (\alpha\beta)_{ij} = 0$ for all i .
- α_i represents the site effect at location i ; β_j is the j -th day effect and γ_k is the hourly effect (diurnal pattern).
- $(\alpha\beta)_{ij}$ is for the effect at site i on day j , $(\alpha\gamma)_{ik}$ is for the effect at site i hour k , and $(\beta\gamma)_{jk}$ is for the effect on day j at hour k .
- In this study, we group overall mean and γ_k as the diurnal effect, since this is the dominant source of variation in the data.

We do this analysis of variance for the differences between CMAQ model output and observations, and compare to the corresponding decomposition for the observations. If CMAQ is able to capture some variation, we would expect to see smaller number in the decomposition of differences than in the observations.

Table 2. ANOVA for the Chicago area study ($\times 10^3$ per site).

	M^{36}	M^{12}	A^{12}	M^4	A^4	X	M^{36}	M^{12}	A^{12}	M^4	A^4	X
Hour												
RL	45	41	45	36	38	864	35	40	34	45	35	91
RH	52	49	71	31	60		38	36	34	34	32	
UL	111	103	38	148	33	737	60	55	49	63	51	109
UH	88	23	15	45	14		70	57	51	56	45	
Day												
RL	8	11	10	7	8	15	48	51	47	50	47	57
RH	13	12	9	9	9		58	60	56	58	53	
UL	30	17	25	16	25	24	88	91	84	90	82	85
UH	39	18	25	16	25		104	100	98	97	93	
Site												
RL	21	24	20	25	19	13	5	3	3	4	3	3
RH	21	20	16	22	16		6	5	4	5	4	
UL	17	24	16	26	16	13	13	10	11	10	11	11
UH	18	23	15	26	14		14	11	11	10	11	
Day×Hour												
RL	207	224	201	227	193	1079	45	54	43	61	43	35
RH	238	245	236	228	219		49	63	46	70	46	
UL	353	339	256	401	252	1010	33	40	33	47	33	31
UH	368	277	250	305	238		36	45	34	55	35	
Site×Day												
RL	21	24	20	25	19	13	5	3	3	4	3	3
RH	21	20	16	22	16		6	5	4	5	4	
UL	17	24	16	26	16	13	13	10	11	10	11	11
UH	18	23	15	26	14		14	11	11	10	11	
Site×Hour												
RL	207	224	201	227	193	1079	45	54	43	61	43	35
RH	238	245	236	228	219		49	63	46	70	46	
UL	353	339	256	401	252	1010	33	40	33	47	33	31
UH	368	277	250	305	238		36	45	34	55	35	
Total												
RL	207	224	201	227	193	1079	45	54	43	61	43	35
RH	238	245	236	228	219		49	63	46	70	46	
UL	353	339	256	401	252	1010	33	40	33	47	33	31
UH	368	277	250	305	238		36	45	34	55	35	
Residual												

2 Case Study Two: Atlanta Area

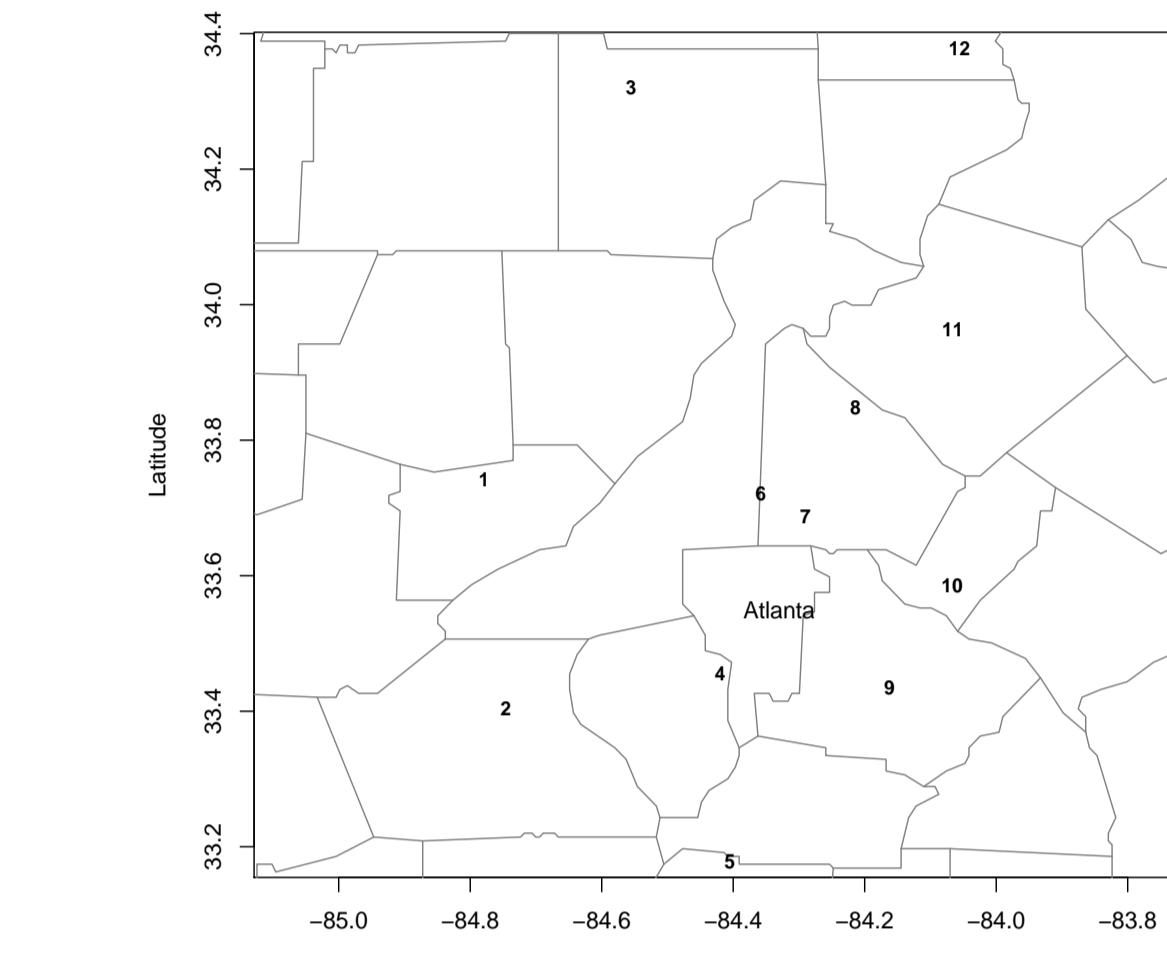


Figure 3: The Atlanta area.

	M^{32}	M^8	A^8	M^2	A^2	X
FB	38	30	30			